

ANOVA with binary variables - The F-test and some Alternatives

Appendix B 4 Tables and Graphs of the Power of selected methods in relation to n_i (5,10,...,50) in mixed designs

All tables refer to $\alpha=0.05$ and $\alpha=0.01$, graphs to $\alpha=0.05$. Reported are the proportions of rejections of the corresponding null hypothesis.

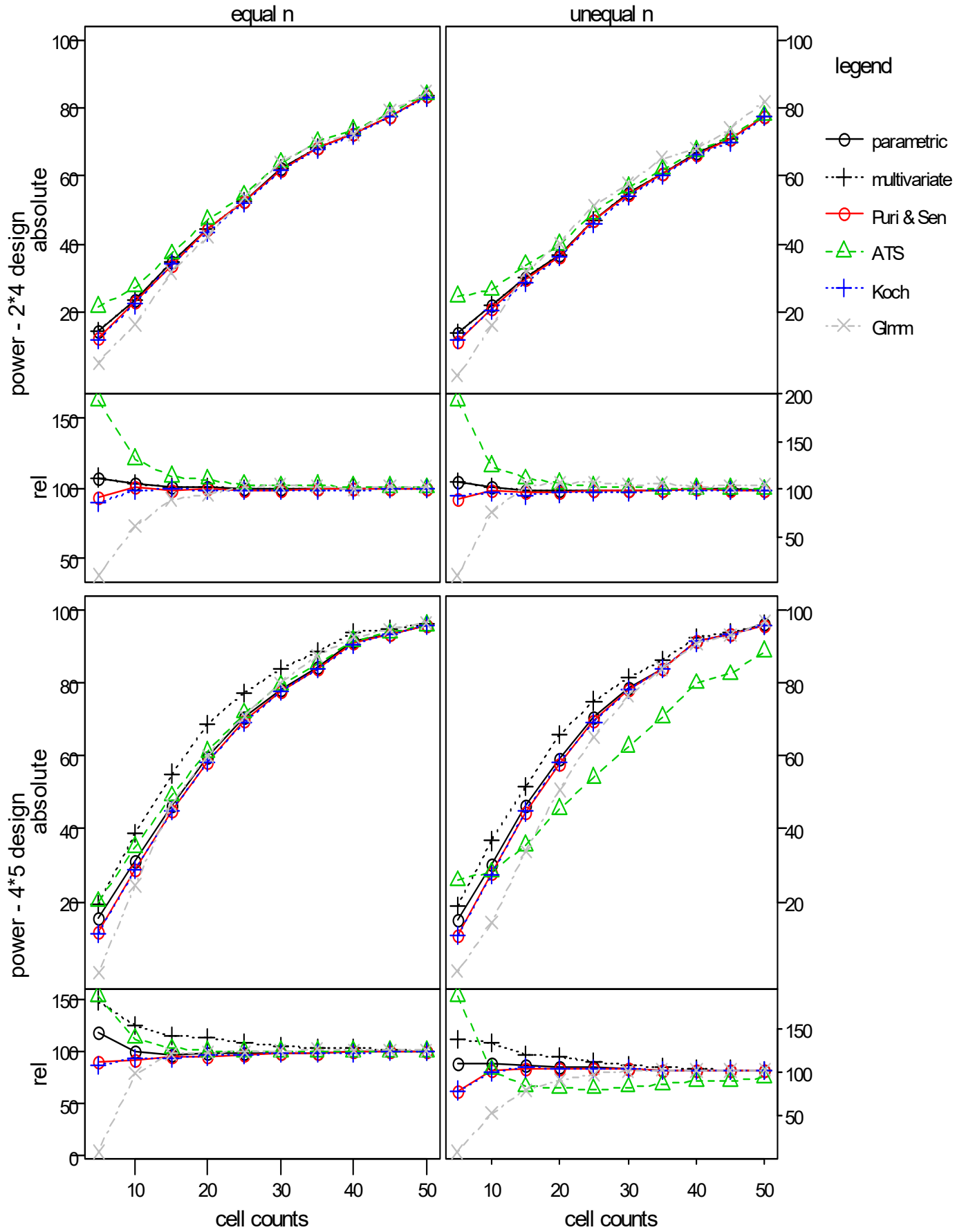
Table of Contents

4. 1. Main effect A (effects $a_i = 0.4*s$)	1
4. 1. 1. equal correlations on B ($r=0.3$)	1
4. 1. 1. 1 $p = 0.5$	1
4. 1. 1. 2 $p = 0.8$	3
4. 1. 1. 3 $p = 0.9$	5
4. 1. 2. unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)	7
4. 1. 2. 1 $p = 0.5$	7
4. 1. 2. 2 $p = 0.8$	9
4. 1. 2. 3 $p = 0.9$	11
4. 2. Main effect B (effects $b_i = 0.3*s$)	13
4. 2. 1. equal correlations on B ($r=0.3$)	13
4. 2. 1. 1 $p = 0.5$	13
4. 2. 1. 2 $p = 0.8$	15
4. 2. 1. 3 $p = 0.9$	17
4. 2. 2. unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)	19
4. 2. 2. 1 $p = 0.5$	19
4. 2. 2. 2 $p = 0.8$	21
4. 2. 2. 3 $p = 0.9$	23
4. 3. Main effect B (effects $b_i = 0.3*s$) A significant (effects $a_i = 0.4*s$) small $n_i \sim$ small p_i and small $n_i \sim$ large p_i	25
4. 3. 1. equal correlations on B ($r=0.3$)	25
4. 3. 1. 1 $p = 0.5$	25
4. 3. 1. 2 $p = 0.8$	27
4. 3. 1. 3 $p = 0.9$	29

4. 3. 2.	unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)	31
4. 3. 2. 1	$p = 0.5$	31
4. 3. 2. 2	$p = 0.8$	33
4. 3. 2. 3	$p = 0.9$	35
4. 4.	Interaction effect AB (effects $ab_{ij} = 0.4*s$)	37
4. 4. 1.	equal correlations on B ($r=0.3$)	37
4. 4. 1. 1	$p = 0.5$	37
4. 4. 1. 2	$p = 0.8$	39
4. 4. 1. 3	$p = 0.9$	41
4. 4. 2.	unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)	43
4. 4. 2. 1	$p = 0.5$	43
4. 4. 2. 2	$p = 0.8$	45
4. 4. 2. 3	$p = 0.9$	47
4. 5.	Interaction effect AB (effects $ab_i = 0.4*s$) A significant (effects $a_i = 0.4*s$) small $n_i \sim$ small p_i and small $n_i \sim$ large p_i	49
4. 5. 1.	equal correlations on B ($r=0.3$)	49
4. 5. 1. 1	$p = 0.5$	49
4. 5. 1. 2	$p = 0.8$	51
4. 5. 1. 3	$p = 0.9$	53
4. 5. 2.	unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)	55
4. 5. 2. 1	$p = 0.5$	55
4. 5. 2. 2	$p = 0.8$	57
4. 5. 2. 3	$p = 0.9$	59

4. 1. Main effect A (effects $a_i = 0.4*s$)**4. 1. 1. equal correlations on B ($r=0.3$)****4. 1. 1. 1 $p = 0.5$**

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	14.25	23.40	34.50	44.40	62.15	72.55	83.25	13.65	21.80	29.85	36.70	55.00	66.55	77.60
	par./ HF-corr.														
	multivariate	14.25	23.40	34.50	44.40	62.15	72.55	83.25	13.65	21.80	29.85	36.70	55.00	66.55	77.60
	Puri & Sen	12.45	22.75	33.90	44.15	61.80	72.30	83.25	11.50	20.90	29.35	36.20	54.60	66.45	77.40
	ATS	21.55	27.25	37.15	47.05	63.85	73.45	83.95	24.60	26.35	33.85	39.85	56.50	67.30	77.85
	Koch	11.95	22.25	33.95	43.35	61.80	71.60	82.95	11.85	20.50	28.40	36.05	54.00	66.30	77.20
	GLMM	5.00	16.40	31.60	42.20	64.00	72.10	84.60	1.20	16.00	31.80	40.10	57.80	67.80	81.90
4*5	parametric	15.40	31.25	46.30	59.45	78.35	91.25	95.55	15.10	30.10	46.30	59.35	78.65	91.45	96.00
	par./ HF-corr.														
	multivariate	19.45	38.90	55.15	68.70	83.85	94.00	96.35	18.90	36.70	51.45	65.85	81.50	92.25	95.95
	Puri & Sen	11.80	28.70	45.10	58.30	77.75	91.00	95.55	10.75	27.95	44.60	58.00	78.05	91.25	95.90
	ATS	20.05	35.05	49.15	61.20	79.50	91.55	95.80	25.80	28.15	35.45	45.40	62.65	80.00	88.65
	Koch	11.40	29.00	44.85	58.40	77.80	90.75	95.70	10.75	27.60	44.75	58.10	78.10	91.25	95.85
	GLMM	0.50	24.60	46.70	60.10	79.90	92.50	96.60	1.00	14.20	33.90	50.70	76.50	90.90	96.80

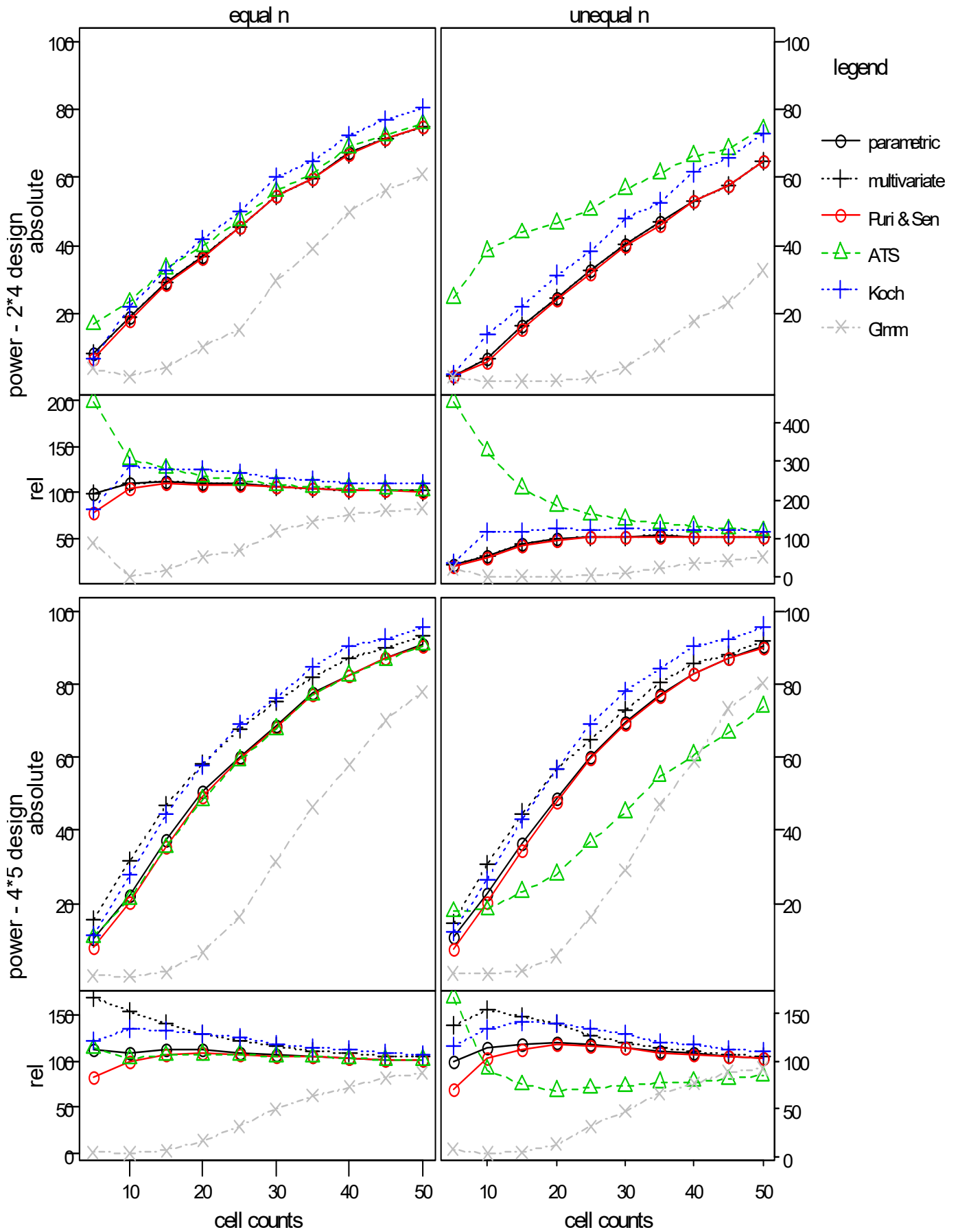


4. 1. 1. 2 p = 0.8

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	12.55	23.55	35.70	45.00	64.50	76.05	84.15	4.45	13.30	25.30	34.30	52.35	64.05	75.80
	par./ HF-corr.														
	multivariate	12.55	23.55	35.70	45.00	64.50	76.05	84.15	4.45	13.30	25.30	34.30	52.35	64.05	75.80
	Puri & Sen	10.10	22.10	34.95	44.70	64.15	76.00	84.05	3.50	12.25	24.55	33.80	51.95	63.65	75.75
	ATS	20.90	27.80	38.80	47.70	65.80	76.80	84.60	30.60	36.65	43.80	48.70	63.40	71.55	80.40
	Koch	11.30	25.95	37.60	47.05	67.20	79.15	86.15	5.60	19.25	29.65	38.45	57.55	69.50	79.00
	GLMM	1.60	3.51	14.33	27.96	56.41	73.75	83.47	0.00	0.20	2.50	9.50	35.90	57.70	73.90
4*5	parametric	14.50	30.00	47.50	61.65	79.85	91.80	96.55	14.15	29.25	46.40	61.80	80.45	91.70	96.20
	par./ HF-corr.														
	multivariate	20.50	38.95	54.75	68.95	84.00	94.00	97.15	18.85	36.80	53.60	67.35	81.80	92.60	96.60
	Puri & Sen	10.90	28.15	46.20	60.45	79.40	91.70	96.50	10.75	26.65	45.05	60.50	79.85	91.40	96.05
	ATS	16.45	30.55	48.10	61.85	80.05	91.95	96.65	22.15	21.45	30.50	39.70	59.60	77.00	87.15
	Koch	14.65	32.15	51.05	65.50	84.05	94.70	97.85	13.30	31.30	50.45	66.10	84.35	94.70	97.60
	GLMM	0.00	3.00	20.40	42.30	77.40	93.10	97.50	0.20	1.10	11.32	32.57	68.64	89.48	96.39

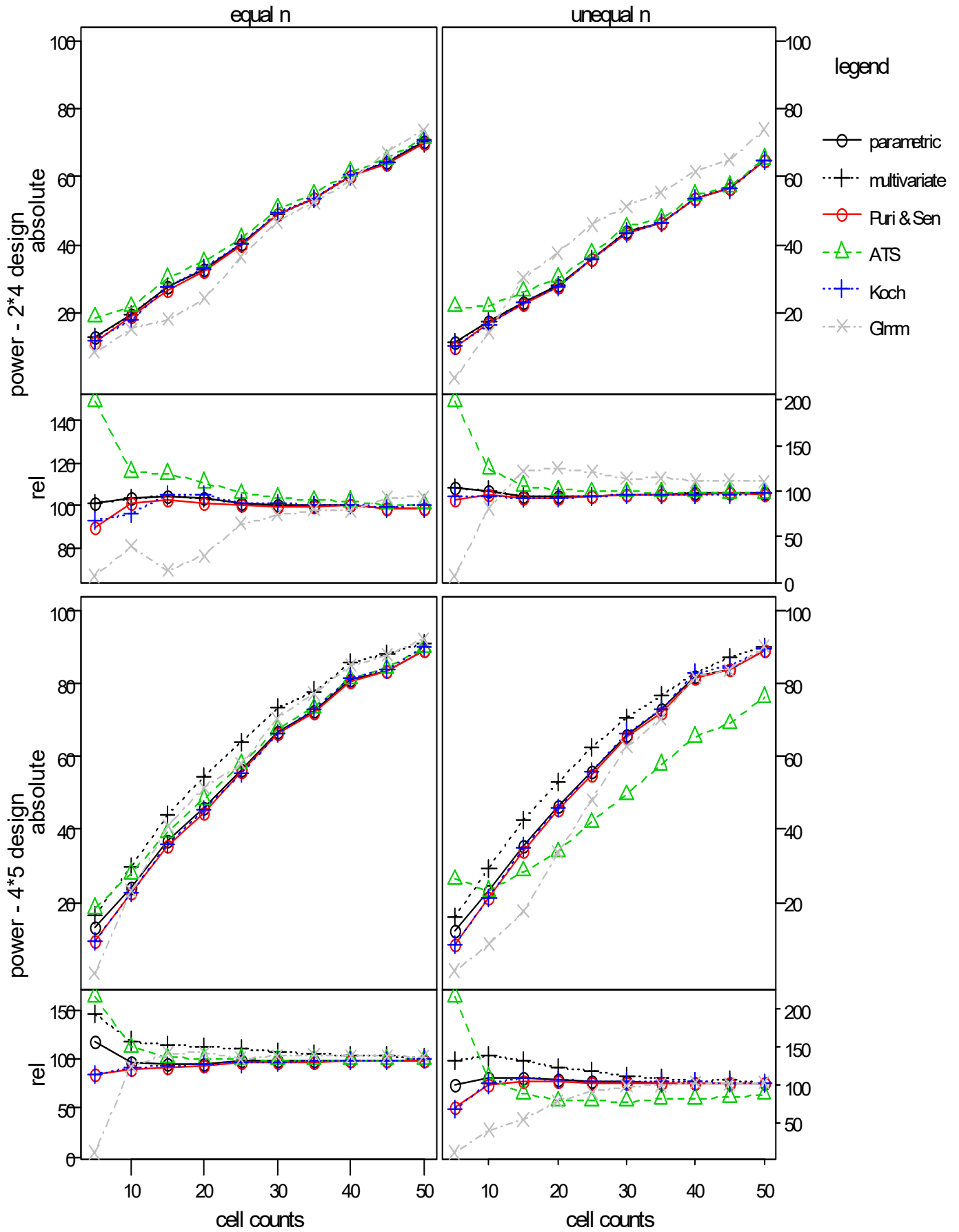
4. 1. 1. 3 $p = 0.9$

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	8.25	18.85	29.25	36.85	54.60	67.00	74.75	1.65	6.50	16.45	24.45	40.05	53.20	64.80
	par./ HF-corr.														
	multivariate	8.25	18.85	29.25	36.85	54.60	67.00	74.75	1.65	6.50	16.45	24.45	40.05	53.20	64.80
	Puri & Sen	6.50	17.85	28.75	36.20	54.40	66.85	74.65	1.40	5.65	15.30	24.05	39.80	53.05	64.65
	ATS	16.75	23.35	33.10	39.65	55.90	68.80	75.70	24.50	38.35	43.75	46.45	56.65	66.25	74.20
	Koch	6.95	22.00	32.65	41.90	59.85	72.45	80.40	1.95	13.70	22.00	31.35	48.10	61.40	72.80
	GLMM	3.82	1.41	4.02	10.06	29.58	49.70	60.66	1.20	0.00	0.10	0.30	4.00	17.80	32.60
4*5	parametric	10.40	22.30	37.45	50.50	68.80	82.60	90.80	10.70	22.80	36.20	48.85	69.60	83.15	90.30
	par./ HF-corr.														
	multivariate	15.70	31.45	46.80	58.35	75.25	87.35	93.35	14.60	30.85	44.70	56.70	73.15	85.90	92.00
	Puri & Sen	7.75	20.50	35.35	49.20	68.05	82.40	90.65	7.60	20.50	34.45	47.80	68.95	82.80	90.10
	ATS	10.60	21.05	35.30	48.25	67.80	82.60	90.70	17.80	18.20	23.15	27.95	45.00	60.75	74.00
	Koch	11.35	27.70	44.30	57.85	76.40	90.60	95.85	12.35	26.60	43.15	56.65	78.15	90.60	95.95
	GLMM	0.20	0.10	1.20	6.50	31.50	58.00	78.10	0.80	0.70	1.41	5.53	29.18	58.95	80.48



4. 1. 2. unequal correlations on B (r = 0.7, 0.5, 0.4, 0.2)**4. 1. 2. 1 p = 0.5**

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	12.55	19.35	27.30	32.80	49.15	60.20	70.05	11.35	17.55	23.15	28.10	43.75	53.55	64.75
	par./ HF-corr.														
	multivariate	12.55	19.35	27.30	32.80	49.15	60.20	70.05	11.35	17.55	23.15	28.10	43.75	53.55	64.75
	Puri & Sen	11.15	18.90	26.75	32.10	48.75	60.00	69.85	10.00	16.75	22.65	27.70	43.40	53.45	64.50
	ATS	18.55	21.65	30.05	35.10	50.65	61.30	71.20	21.70	21.75	26.25	30.30	45.10	54.55	65.15
	Koch	11.55	17.95	27.40	33.20	49.40	60.40	70.75	10.30	16.55	22.80	27.75	43.50	53.40	64.70
	GLMM	8.30	15.10	18.10	24.20	46.70	58.60	73.70	0.80	14.10	30.30	37.50	51.30	61.40	73.80
4*5	parametric	13.30	24.30	36.80	45.90	66.80	81.00	89.30	12.25	23.25	35.35	46.40	66.05	81.80	89.25
	par./ HF-corr.														
	multivariate	16.50	29.65	43.95	54.50	73.25	85.65	90.85	16.00	29.15	42.75	53.10	70.50	83.05	90.05
	Puri & Sen	9.45	22.50	35.50	44.70	66.15	80.60	89.10	8.50	21.20	33.90	45.40	65.40	81.30	89.20
	ATS	18.50	28.00	39.05	48.40	67.55	81.40	89.80	26.30	23.20	28.55	33.85	49.60	65.35	76.35
	Koch	9.50	22.80	35.80	45.50	66.50	81.35	90.00	8.35	21.40	35.20	46.05	66.55	82.80	89.65
	GLMM	0.50	23.12	40.84	51.55	70.47	84.88	92.29	1.30	8.60	17.50	33.80	62.70	81.90	90.20

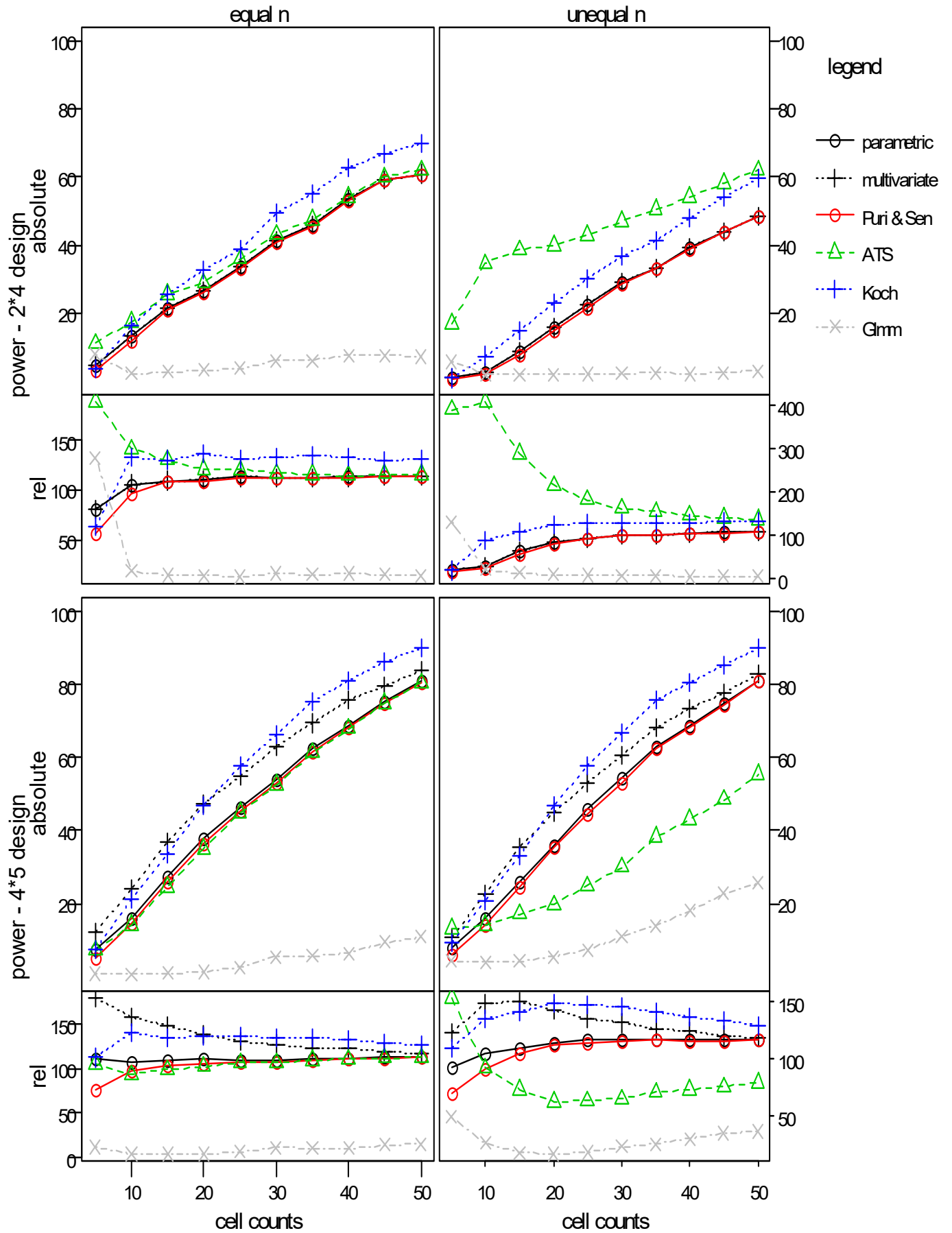


4. 1. 2. 2 $p = 0.8$

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	9.30	17.80	28.15	33.70	50.10	61.55	71.15	2.95	8.95	17.55	24.60	38.05	49.25	60.20
	par./ HF-corr.														
	multivariate	9.30	17.80	28.15	33.70	50.10	61.55	71.15	2.95	8.95	17.55	24.60	38.05	49.25	60.20
	Puri & Sen	7.20	16.75	27.30	33.45	49.75	61.40	71.00	2.05	7.90	16.75	24.05	37.90	49.00	60.00
	ATS	16.50	21.15	30.80	36.00	51.85	62.85	72.40	26.85	33.80	36.20	40.50	50.50	60.50	68.95
	Koch	7.65	20.55	30.35	37.05	54.25	67.10	76.00	2.60	14.20	21.15	28.60	43.55	55.15	66.65
	GLMM	4.12	3.11	8.63	13.65	28.92	36.04	42.27	2.13	1.72	2.13	3.75	11.97	23.12	34.28
4*5	parametric	10.90	22.45	35.45	48.40	65.50	79.85	90.05	11.10	21.60	34.80	47.80	66.90	80.25	89.50
	par./ HF-corr.														
	multivariate	16.65	30.10	44.60	55.50	73.65	86.20	91.75	15.10	28.55	42.80	54.10	71.35	83.30	90.10
	Puri & Sen	8.10	19.80	33.60	46.90	64.85	79.60	90.00	8.65	19.65	33.50	46.80	66.05	79.95	89.40
	ATS	11.95	22.40	35.45	48.45	65.50	80.00	90.05	18.45	16.85	22.30	27.60	43.85	59.35	73.80
	Koch	11.90	25.10	40.55	52.90	73.45	88.10	93.45	11.25	24.85	40.35	54.35	73.60	88.15	93.10
	GLMM	0.00	1.50	9.10	21.20	47.30	68.40	81.60	2.77	3.80	7.70	18.79	47.84	72.18	87.68

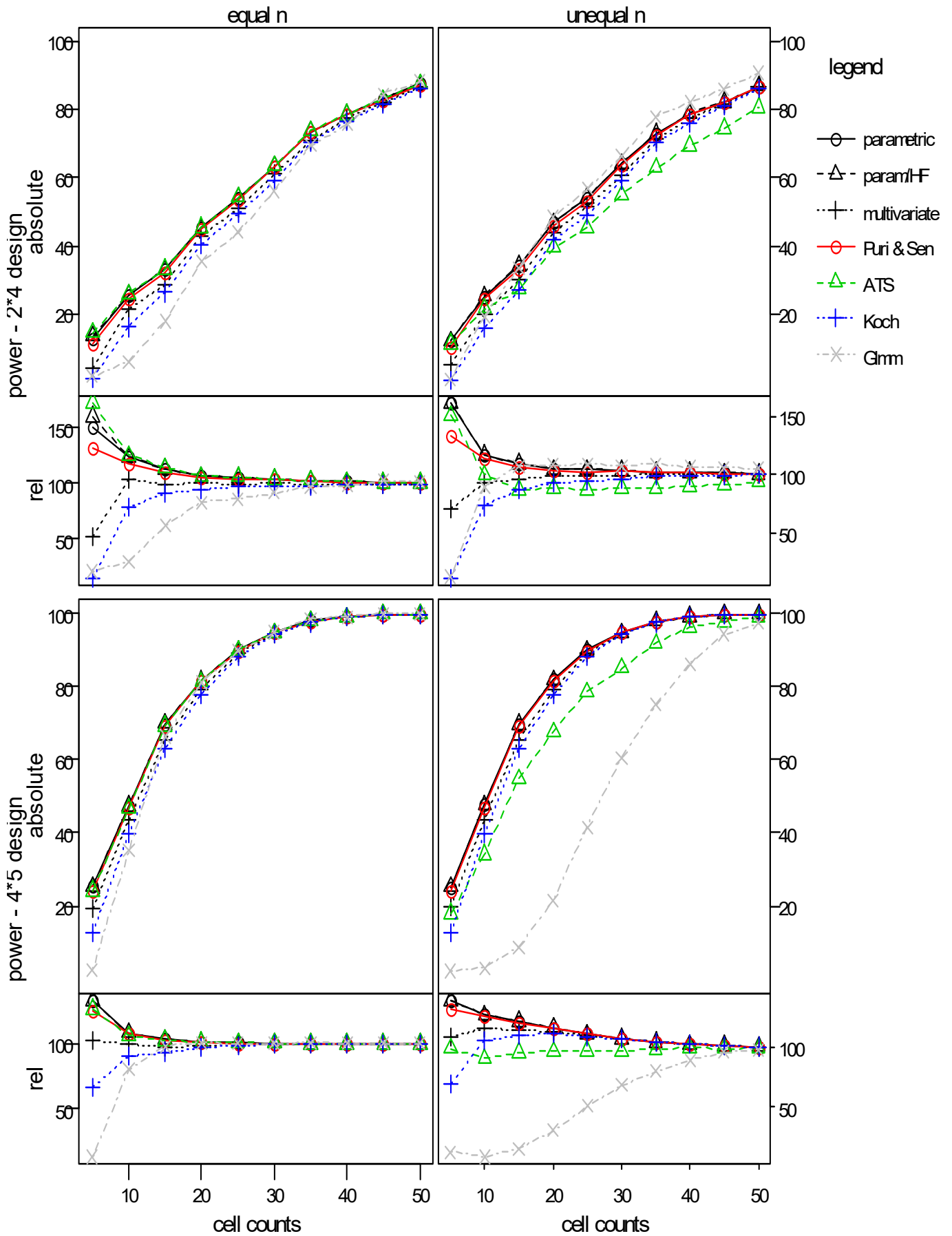
4. 1. 2. 3 p = 0.9

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	4.75	13.10	21.40	26.50	41.25	53.35	60.85	0.95	2.45	8.65	15.60	29.15	39.20	48.35
	par./ HF-corr.														
	multivariate	4.75	13.10	21.40	26.50	41.25	53.35	60.85	0.95	2.45	8.65	15.60	29.15	39.20	48.35
	Puri & Sen	3.30	11.95	21.10	25.80	41.00	53.10	60.60	0.70	2.00	7.55	15.00	28.65	38.90	48.25
	ATS	11.15	17.50	25.50	28.90	43.10	54.15	61.95	16.95	34.55	38.60	39.80	47.00	53.95	62.05
	Koch	3.75	16.50	25.50	32.70	49.25	62.50	69.80	0.85	7.45	14.70	23.00	36.90	48.10	59.75
	GLMM	7.85	2.31	2.82	3.32	5.94	7.65	7.24	5.71	1.94	1.94	2.04	2.34	2.14	2.96
4*5	parametric	7.60	16.25	27.35	37.95	54.15	68.65	80.90	7.95	15.95	25.90	36.05	54.30	68.65	80.95
	par./ HF-corr.														
	multivariate	12.25	24.00	36.80	47.45	62.90	75.90	84.00	10.60	22.60	35.30	45.20	60.65	73.30	82.85
	Puri & Sen	5.25	14.80	25.90	36.40	53.25	68.10	80.65	6.00	13.90	24.65	35.50	53.20	68.20	80.90
	ATS	7.20	14.15	24.65	35.05	52.70	67.90	80.40	13.20	14.10	17.20	19.70	29.95	43.10	55.40
	Koch	7.65	21.35	33.55	46.80	66.35	81.15	90.15	9.40	20.70	33.20	46.70	66.95	80.55	90.15
	GLMM	0.80	0.60	1.01	1.31	5.53	6.33	10.85	4.26	4.05	4.37	5.41	10.91	17.98	25.68



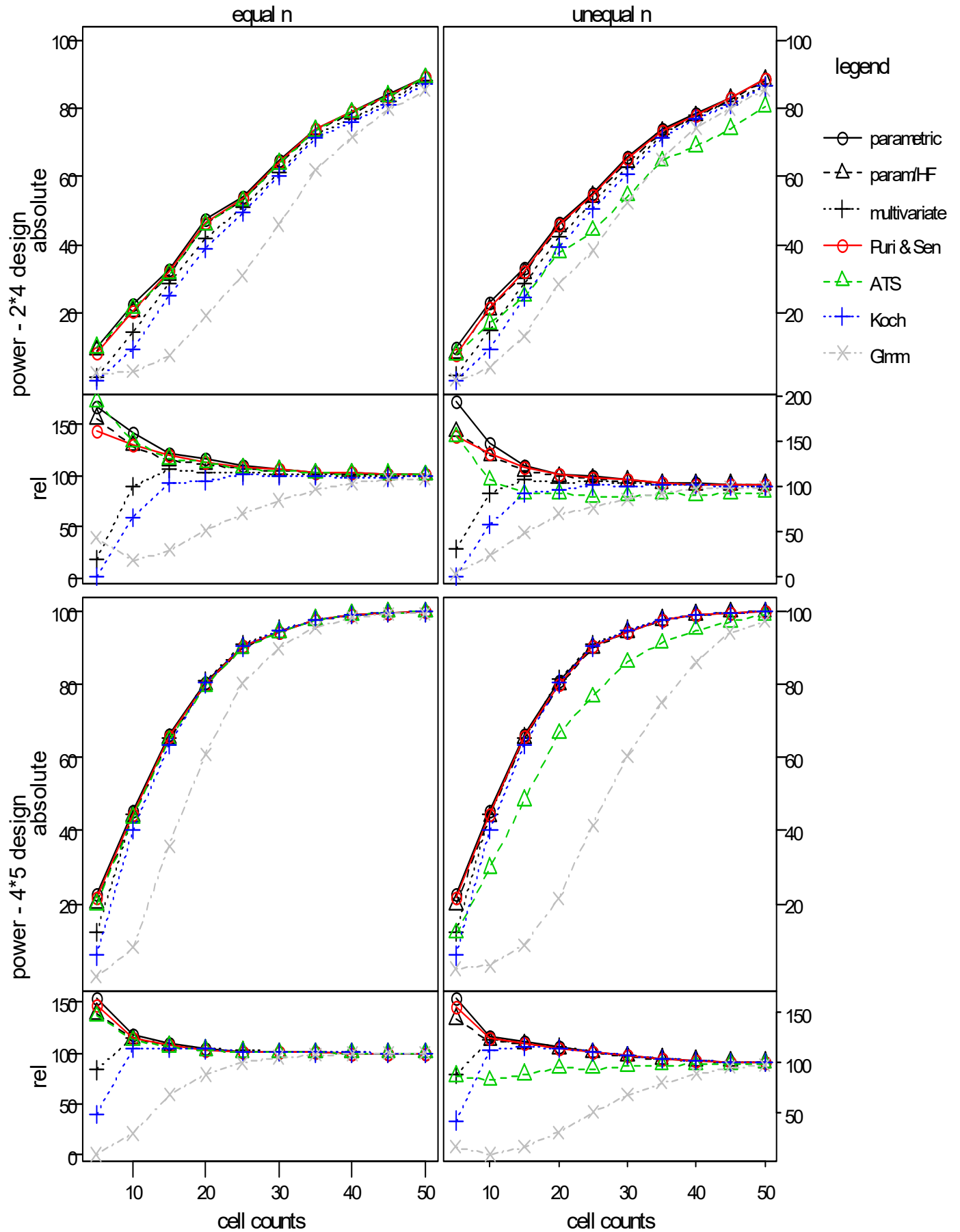
4. 2. Main effect B (effects $b_i = 0.3*s$)**4. 2. 1. equal correlations on B ($r=0.3$)****4. 2. 1. 1 $p = 0.5$**

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	12.75	25.60	32.95	45.55	63.15	78.55	87.40	12.20	25.20	34.20	47.10	64.30	78.60	86.80
	par./ HF-corr.	13.50	25.60	32.95	45.25	63.35	78.55	87.40	12.20	25.30	34.30	46.70	64.00	78.70	86.75
	multivariate	4.40	21.55	28.70	42.95	61.10	77.15	86.30	5.30	20.15	29.85	44.00	60.80	77.35	86.65
	Puri & Sen	11.10	24.45	32.15	44.85	62.95	78.25	87.05	10.10	24.50	33.30	46.10	63.85	78.30	86.70
	ATS	14.55	25.90	33.20	45.35	63.35	78.55	87.40	11.40	21.60	27.20	39.45	54.80	69.30	80.60
	Koch	1.20	16.15	26.30	40.30	59.25	76.45	85.85	0.80	15.75	27.10	41.65	59.30	76.10	86.20
	GLMM	1.72	6.05	17.86	35.42	56.00	75.48	88.19	0.90	19.30	33.60	48.40	66.20	82.00	90.60
4*5	parametric	25.35	47.40	69.75	81.60	94.75	99.05	99.75	25.25	47.60	69.60	81.80	94.75	99.05	99.75
	par./ HF-corr.	25.35	47.40	69.85	81.60	94.75	99.00	99.75	25.25	47.55	69.70	81.85	94.75	99.05	99.70
	multivariate	19.50	43.55	65.25	79.25	94.55	98.95	99.70	19.65	43.60	65.55	79.15	94.50	98.90	99.70
	Puri & Sen	23.85	47.05	69.00	81.60	94.75	99.05	99.75	23.85	47.05	69.00	81.60	94.75	99.05	99.75
	ATS	24.05	46.55	69.20	81.45	94.75	99.00	99.75	17.95	34.05	54.80	67.60	85.05	96.25	98.90
	Koch	12.60	39.70	63.20	77.95	94.15	98.90	99.70	12.60	39.70	63.20	77.95	94.15	98.90	99.70
	GLMM	2.50	35.20	66.30	81.00	94.80	98.90	99.90	2.24	3.06	8.67	21.63	60.41	86.12	97.24



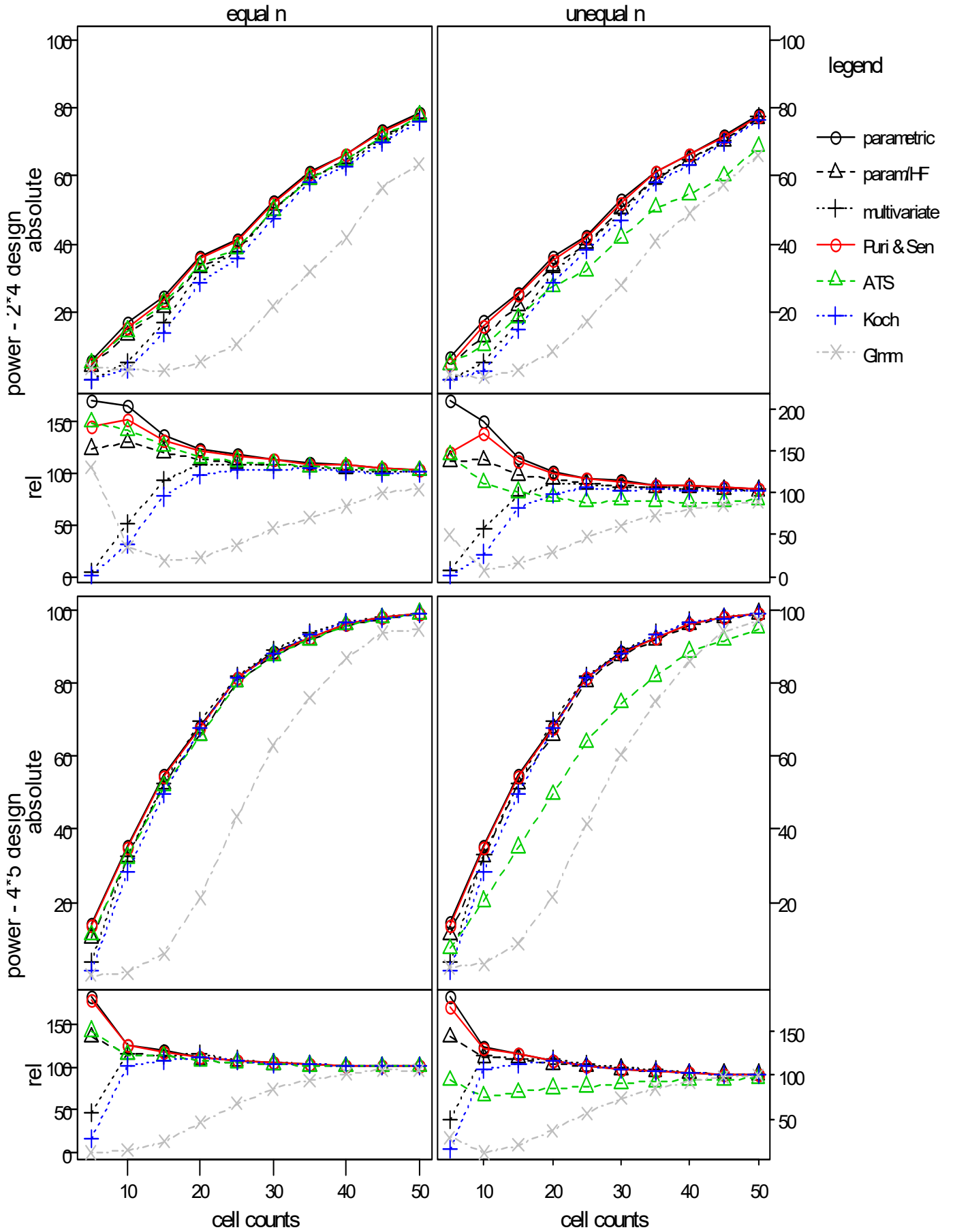
4. 2. 1. 2 $p = 0.8$

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	9.60	22.45	32.45	47.35	64.60	79.05	89.15	9.75	23.10	33.20	46.45	65.60	78.25	88.55
	par./ HF-corr.	8.90	20.50	30.90	45.70	63.45	78.65	88.75	8.10	20.95	31.60	45.10	64.30	77.55	88.25
	multivariate	1.05	14.25	28.45	41.90	61.25	77.00	87.85	1.55	14.60	28.75	42.35	62.50	77.90	86.75
	Puri & Sen	8.25	20.55	31.95	46.50	64.25	78.90	89.10	7.85	21.40	32.35	45.85	65.20	77.95	88.40
	ATS	9.85	21.15	31.35	45.90	63.65	78.70	88.85	7.80	16.85	24.70	37.75	54.25	68.80	80.40
	Koch	0.10	9.35	25.10	38.90	59.95	75.95	87.20	0.05	9.15	24.70	39.30	60.70	76.80	86.30
	GLMM	2.23	2.74	7.31	19.09	45.89	71.37	85.28	0.20	3.80	13.20	28.40	52.40	74.10	85.40
4*5	parametric	22.55	45.65	66.35	80.65	94.55	99.05	99.85	22.75	45.65	66.50	80.85	94.55	99.05	99.85
	par./ HF-corr.	20.25	44.00	65.10	79.90	94.35	99.05	99.85	19.90	43.85	65.25	79.85	94.35	99.05	99.85
	multivariate	12.15	44.30	65.50	81.20	95.00	99.10	99.80	12.25	44.30	65.60	81.30	95.00	99.10	99.80
	Puri & Sen	21.55	44.60	65.75	80.20	94.50	99.05	99.85	21.55	44.60	65.75	80.20	94.50	99.05	99.85
	ATS	19.95	43.50	64.85	79.65	94.30	99.05	99.85	11.95	29.75	48.40	66.60	86.15	94.95	98.85
	Koch	5.85	40.30	63.30	80.35	94.80	99.10	99.80	5.85	40.30	63.30	80.35	94.80	99.10	99.80
	GLMM	0.00	8.00	35.80	61.00	90.00	98.30	99.40	2.24	3.06	8.67	21.63	60.41	86.12	97.24



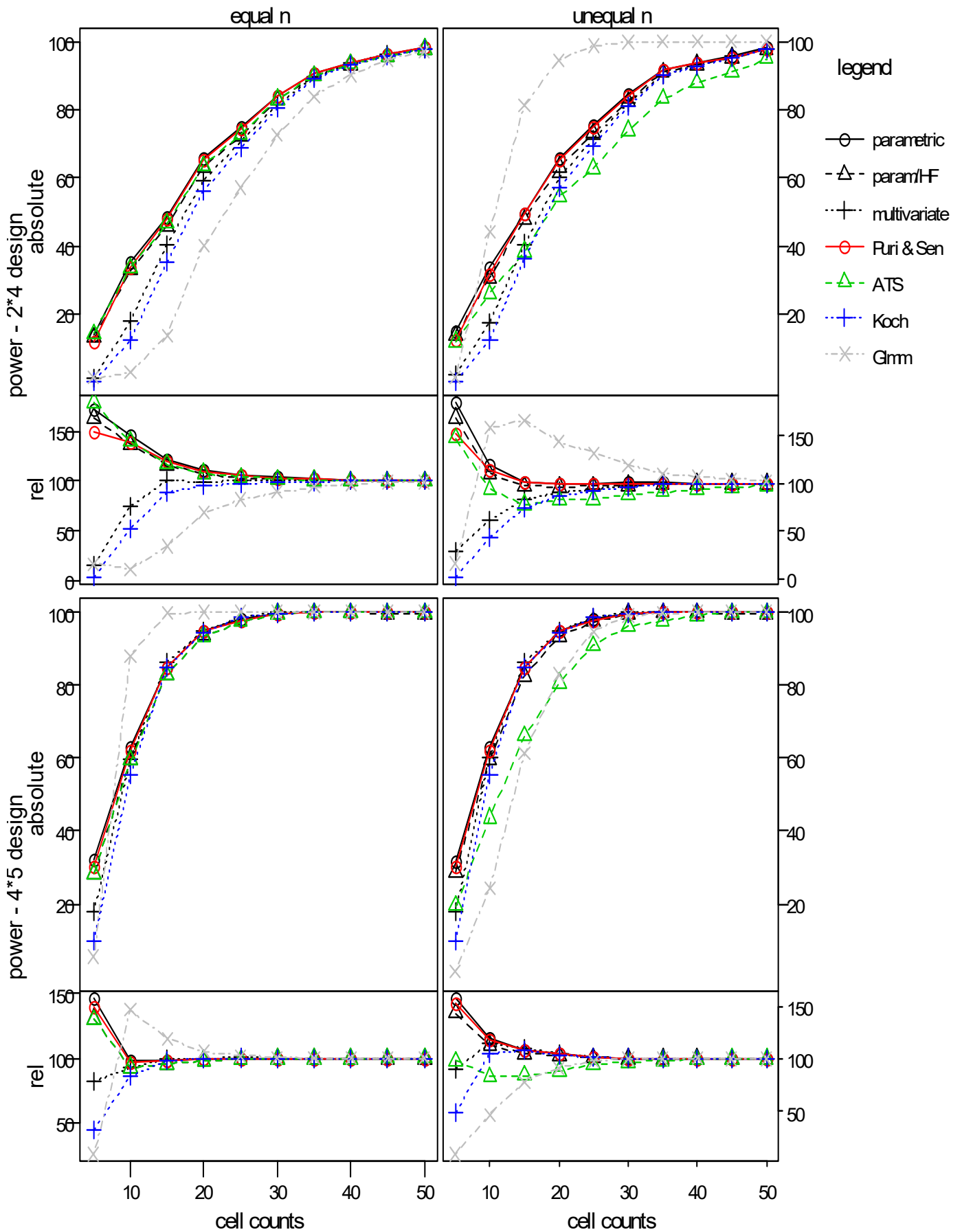
4. 2. 1. 3 p = 0.9

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	5.70	16.80	24.30	36.10	52.30	66.25	78.20	6.85	17.20	25.65	36.40	52.80	66.25	77.70
	par./ HF-corr.	4.15	13.15	21.45	33.25	49.85	64.60	77.50	4.50	12.90	21.90	33.50	50.20	64.80	76.75
	multivariate	0.15	5.25	16.65	31.50	49.70	63.60	76.80	0.25	5.30	17.45	31.80	49.00	64.45	77.15
	Puri & Sen	4.85	15.40	23.45	35.60	52.00	66.05	78.00	4.80	15.80	24.95	35.35	52.20	66.05	77.35
	ATS	5.00	14.40	22.50	33.40	49.95	64.75	77.60	4.75	10.35	18.25	27.45	41.90	54.55	68.40
	Koch	0.05	3.25	13.85	28.80	47.40	62.45	76.05	0.05	2.50	14.90	28.50	47.00	63.15	76.50
	GLMM	3.56	2.95	2.85	5.39	21.65	41.77	63.41	1.60	0.70	3.01	8.32	27.86	48.90	66.13
4*5	parametric	14.15	35.50	54.90	68.10	88.50	96.15	99.20	14.70	35.70	54.80	68.15	88.50	96.15	99.20
	par./ HF-corr.	10.45	32.35	52.35	65.85	87.65	95.90	99.20	11.10	32.30	52.45	65.95	87.70	95.90	99.15
	multivariate	3.65	32.75	52.40	69.65	88.90	96.80	99.20	3.85	32.90	52.45	69.45	88.85	96.90	99.20
	Puri & Sen	13.75	35.05	54.40	67.70	88.30	96.05	99.20	13.75	35.05	54.40	67.70	88.30	96.05	99.20
	ATS	11.00	32.15	51.80	65.60	87.65	95.90	99.20	7.25	20.25	35.10	49.60	74.55	88.60	95.00
	Koch	1.25	28.40	49.65	67.95	88.25	96.75	99.15	1.25	28.40	49.65	67.95	88.25	96.75	99.15
	GLMM	0.00	0.70	6.00	21.20	63.00	86.80	94.80	2.24	3.06	8.67	21.63	60.41	86.12	97.24



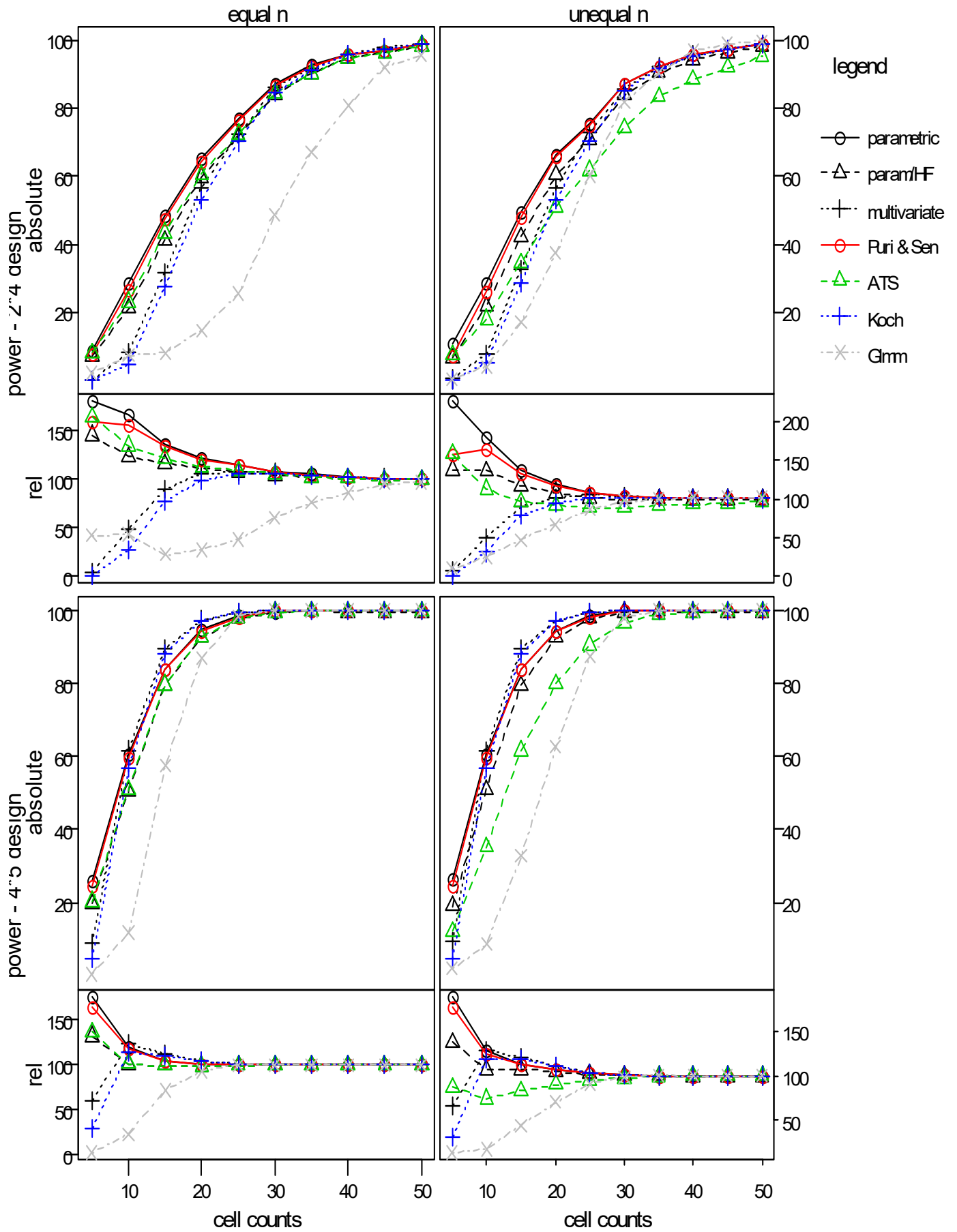
4. 2. 2. unequal correlations on B (r = 0.7, 0.5, 0.4, 0.2)**4. 2. 2. 1 p = 0.5**

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	13.65	35.00	48.30	65.65	84.05	93.70	98.20	14.85	33.40	49.65	65.45	84.35	93.80	98.00
	par./ HF-corr.	13.05	32.85	45.95	63.30	82.90	93.30	97.80	13.55	30.55	47.70	63.25	82.40	93.15	97.50
	multivariate	1.25	17.90	40.25	58.85	81.60	93.65	97.95	2.30	17.25	40.50	60.00	82.05	93.25	97.95
	Puri & Sen	11.90	33.60	47.70	65.00	83.80	93.60	98.05	12.30	31.65	49.35	65.05	84.15	93.70	97.90
	ATS	14.25	33.55	46.55	63.60	83.10	93.35	97.80	11.85	25.95	38.35	54.40	73.85	87.90	94.90
	Koch	0.25	12.35	35.35	56.00	80.55	93.20	97.90	0.15	12.10	36.40	57.30	80.80	92.75	97.70
	GLMM	1.30	2.70	13.70	40.00	72.50	90.10	97.00	1.30	43.90	81.40	94.60	99.80	99.90	100.00
4*5	parametric	31.95	63.20	85.05	94.75	99.60	99.95	99.95	31.55	63.10	85.00	94.70	99.65	99.95	99.95
	par./ HF-corr.	28.45	59.70	82.75	93.55	99.55	99.95	99.95	28.65	59.55	82.60	93.45	99.55	99.95	99.95
	multivariate	17.80	59.90	86.25	94.75	99.80	99.95	99.95	17.85	60.10	86.10	94.65	99.80	99.95	99.95
	Puri & Sen	30.45	62.15	84.65	94.70	99.60	99.95	99.95	30.45	62.15	84.65	94.70	99.60	99.95	99.95
	ATS	28.35	59.40	82.85	93.40	99.55	99.95	99.95	19.50	43.50	66.00	80.60	96.15	99.05	99.90
	Koch	9.70	55.60	84.65	94.30	99.75	99.95	99.95	9.70	55.60	84.65	94.30	99.75	99.95	99.95
	GLMM	5.60	88.10	99.60	100.0	100.0	100.0	100.0	1.70	24.30	61.20	82.90	99.10	100.0	100.00



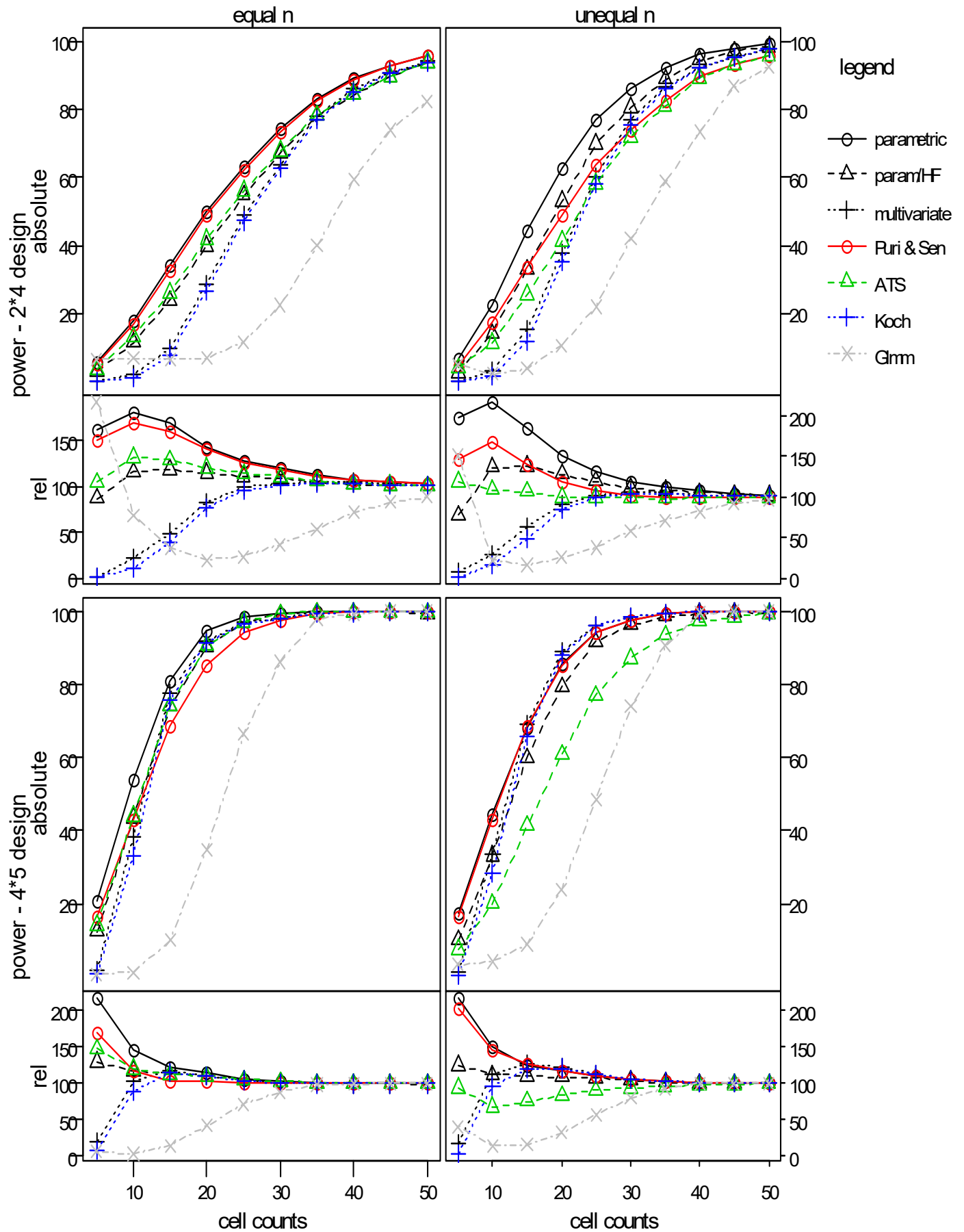
4. 2. 2. 2 p = 0.8

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	8.95	28.45	48.25	65.05	86.95	95.65	98.55	10.65	28.70	49.20	66.45	86.90	95.80	98.85
	par./ HF-corr.	7.20	21.10	41.20	59.60	84.00	94.55	98.30	6.45	21.80	42.05	60.30	83.75	94.20	98.10
	multivariate	0.25	8.40	31.70	56.50	85.80	95.80	98.75	0.35	7.85	32.70	56.60	85.75	95.45	98.95
	Puri & Sen	7.90	26.60	47.50	64.00	86.80	95.55	98.55	7.45	26.25	47.95	65.80	86.85	95.70	98.90
	ATS	8.15	23.05	43.35	60.40	84.40	94.70	98.30	7.45	17.95	34.60	51.05	74.15	88.25	95.15
	Koch	0.05	4.65	27.60	53.10	84.35	95.65	98.70	0.05	4.95	28.50	52.90	85.00	95.35	98.70
	GLMM	2.11	7.44	8.15	14.69	48.59	80.58	95.27	0.50	4.01	16.93	37.37	81.76	96.69	99.60
4*5	parametric	26.20	60.60	83.95	94.65	99.75	99.95	99.95	26.30	60.75	83.80	94.55	99.80	99.95	99.95
	par./ HF-corr.	19.65	50.55	79.70	92.60	99.60	99.95	99.95	19.10	51.05	79.55	92.65	99.55	99.95	99.95
	multivariate	9.00	61.80	89.55	97.40	99.85	99.95	99.95	9.20	61.45	89.40	97.30	99.85	99.95	99.95
	Puri & Sen	24.50	59.60	83.70	94.55	99.80	99.95	99.95	24.50	59.60	83.70	94.55	99.80	99.95	99.95
	ATS	20.30	51.00	79.65	92.70	99.60	99.95	99.95	12.10	35.20	61.60	79.90	96.70	99.65	99.95
	Koch	4.45	56.90	88.15	97.20	99.85	99.95	99.95	4.45	56.90	88.15	97.20	99.85	99.95	99.95
	GLMM	0.40	11.75	57.53	86.95	100.0	100.0	100.0	1.93	8.54	32.83	62.70	97.97	100.0	100.00



4. 2. 2. 3 p = 0.9

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	5.45	18.00	34.05	49.95	74.15	89.00	95.70	6.65	22.60	44.50	62.75	85.95	96.35	99.10
	par./ HF-corr.	2.95	11.50	23.85	39.80	67.00	84.25	93.65	2.60	14.25	33.00	53.10	80.60	94.35	98.35
	multivariate	0.05	2.15	9.95	28.75	63.85	86.05	94.15	0.25	3.00	15.25	37.70	77.00	92.05	97.85
	Puri & Sen	5.10	16.75	32.40	49.05	73.35	88.55	95.55	4.90	17.60	33.55	48.75	73.80	89.55	95.80
	ATS	3.55	13.10	26.05	41.75	67.80	84.65	93.70	4.00	11.35	25.60	41.25	71.80	89.20	95.70
	Koch	0.05	1.05	7.95	26.55	62.45	85.00	93.85	0.05	1.75	11.60	35.30	75.60	91.90	97.85
	GLMM	6.49	6.80	6.59	6.90	22.41	59.33	82.25	5.07	2.33	3.85	10.65	41.99	73.33	92.49
4*5	parametric	20.85	54.00	81.00	94.60	99.65	99.95	99.95	17.55	44.35	68.35	85.55	97.75	99.95	99.95
	par./ HF-corr.	12.40	43.55	74.10	90.65	99.35	99.95	99.95	10.05	33.10	60.10	79.40	96.40	99.65	99.95
	multivariate	1.90	38.20	77.75	92.15	98.25	99.95	99.95	1.45	33.40	69.30	89.10	98.60	99.95	99.95
	Puri & Sen	16.30	43.20	68.75	85.25	97.75	99.95	99.95	16.30	43.20	68.75	85.25	97.75	99.95	99.95
	ATS	14.10	44.15	74.25	90.70	99.35	99.95	99.95	7.60	20.05	41.35	60.90	87.20	97.40	99.55
	Koch	0.70	33.00	76.00	91.60	98.25	99.80	99.90	0.25	28.25	65.90	88.30	98.55	99.85	99.95
	GLMM	0.60	1.20	9.94	34.64	86.24	99.50	100.0	3.30	4.13	8.88	23.94	73.99	99.69	100.00

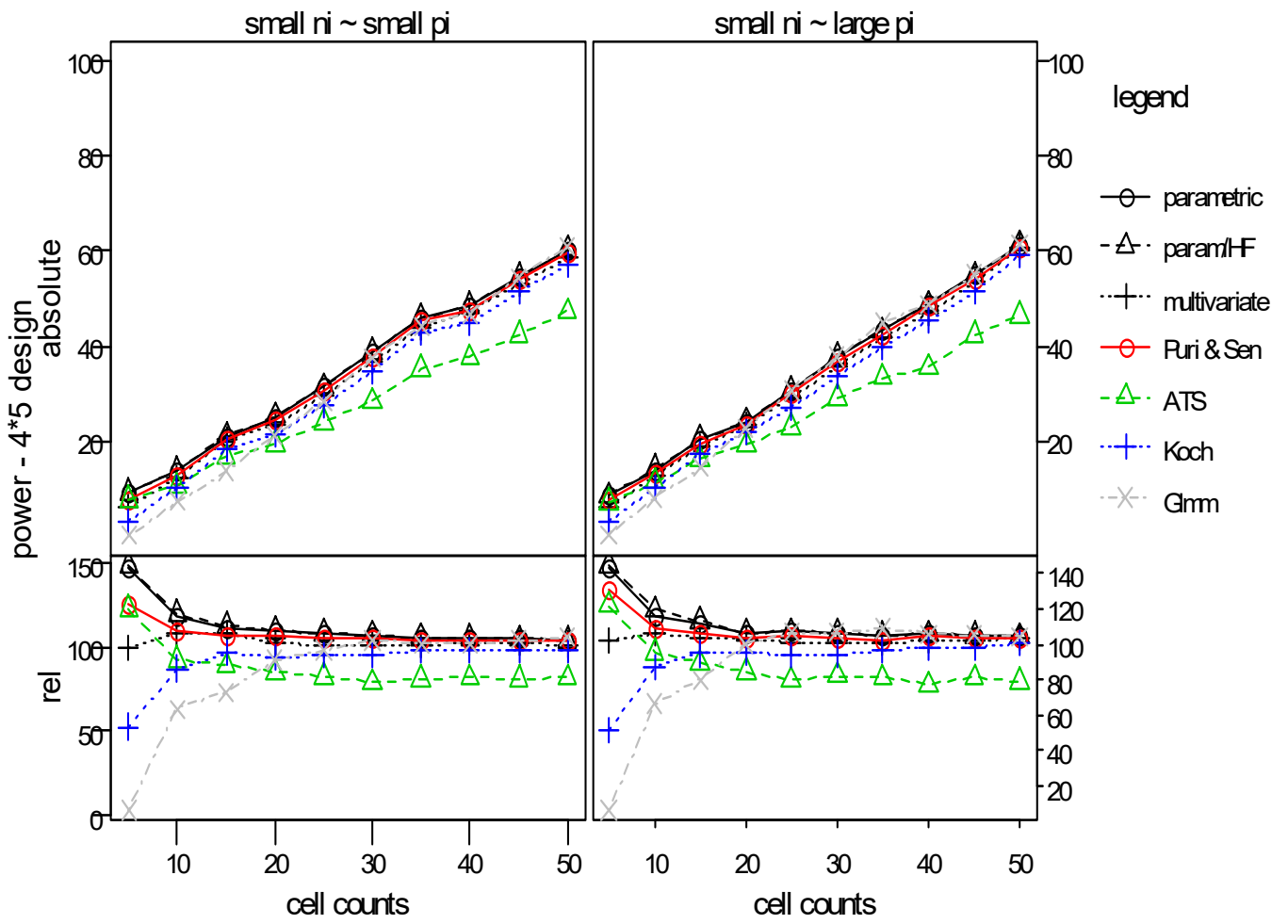


4. 3. Main effect B (effects $b_i = 0.3*s$)
A significant (effects $a_i = 0.4*s$)
small $n_i \sim$ small p_i and small $n_i \sim$ large p_i

4. 3. 1. equal correlations on B ($r=0.3$)

4. 3. 1. 1 $p = 0.5$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	9.20	13.75	21.05	25.25	38.55	48.30	60.30	8.60	13.95	20.35	24.10	37.75	49.00	61.35
	par./ HF-corr.	9.30	13.90	21.25	25.25	38.70	48.40	60.30	8.65	14.35	20.55	24.20	37.70	48.85	61.30
	multivariate	6.25	12.45	20.35	23.50	36.65	47.15	58.80	6.10	12.70	18.80	23.40	35.60	46.85	60.85
	Puri & Sen	7.85	12.75	20.20	24.40	37.75	47.40	59.75	7.80	13.10	19.30	23.50	36.65	48.25	60.80
	ATS	7.70	10.70	16.80	19.50	28.45	37.50	47.20	7.30	11.45	16.20	19.25	29.10	35.45	46.50
	Koch	3.30	10.10	18.20	21.55	34.60	44.75	56.90	3.10	10.40	17.15	21.75	33.50	45.40	59.25
	GLMM	0.20	7.30	13.80	21.20	37.50	46.80	61.00	0.40	8.00	14.50	22.80	37.70	48.80	61.20

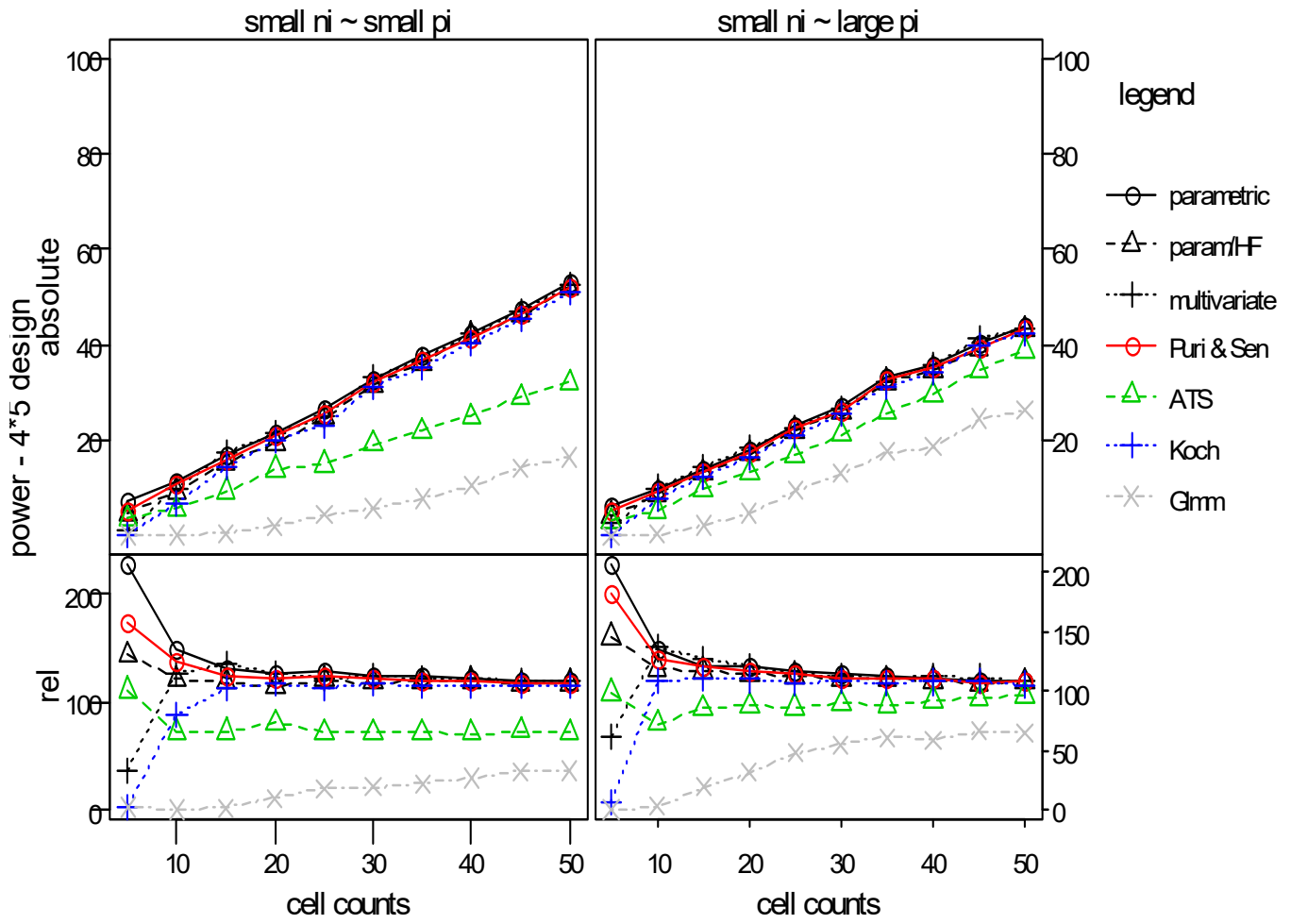


4. 3. 1. 2 $p = 0.8$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	8.15	14.75	22.20	27.60	39.90	51.65	62.25	7.05	13.65	17.30	24.00	33.90	47.7	57.20
	par./ HF-corr.	6.90	13.50	21.20	26.50	38.95	50.70	61.85	6.20	12.80	16.65	23.20	33.40	47.3	57.05
	multivariate	3.80	13.60	19.45	27.00	39.50	51.50	62.40	4.70	13.60	16.30	23.85	33.25	46.8	56.35
	Puri & Sen	7.10	13.90	20.70	26.30	38.85	50.25	61.55	6.50	13.05	16.75	23.20	33.10	47.2	56.70
	ATS	5.20	9.75	13.45	17.30	25.25	34.15	41.15	4.50	9.35	13.05	18.45	27.85	39.7	48.85
	Koch	1.40	10.95	16.80	24.85	37.05	49.25	60.40	1.65	11.15	14.50	21.65	31.15	44.6	54.30
	GLMM	0.10	1.30	2.80	7.91	17.52	26.63	34.53	0.10	2.60	7.40	13.20	22.90	33.0	45.30

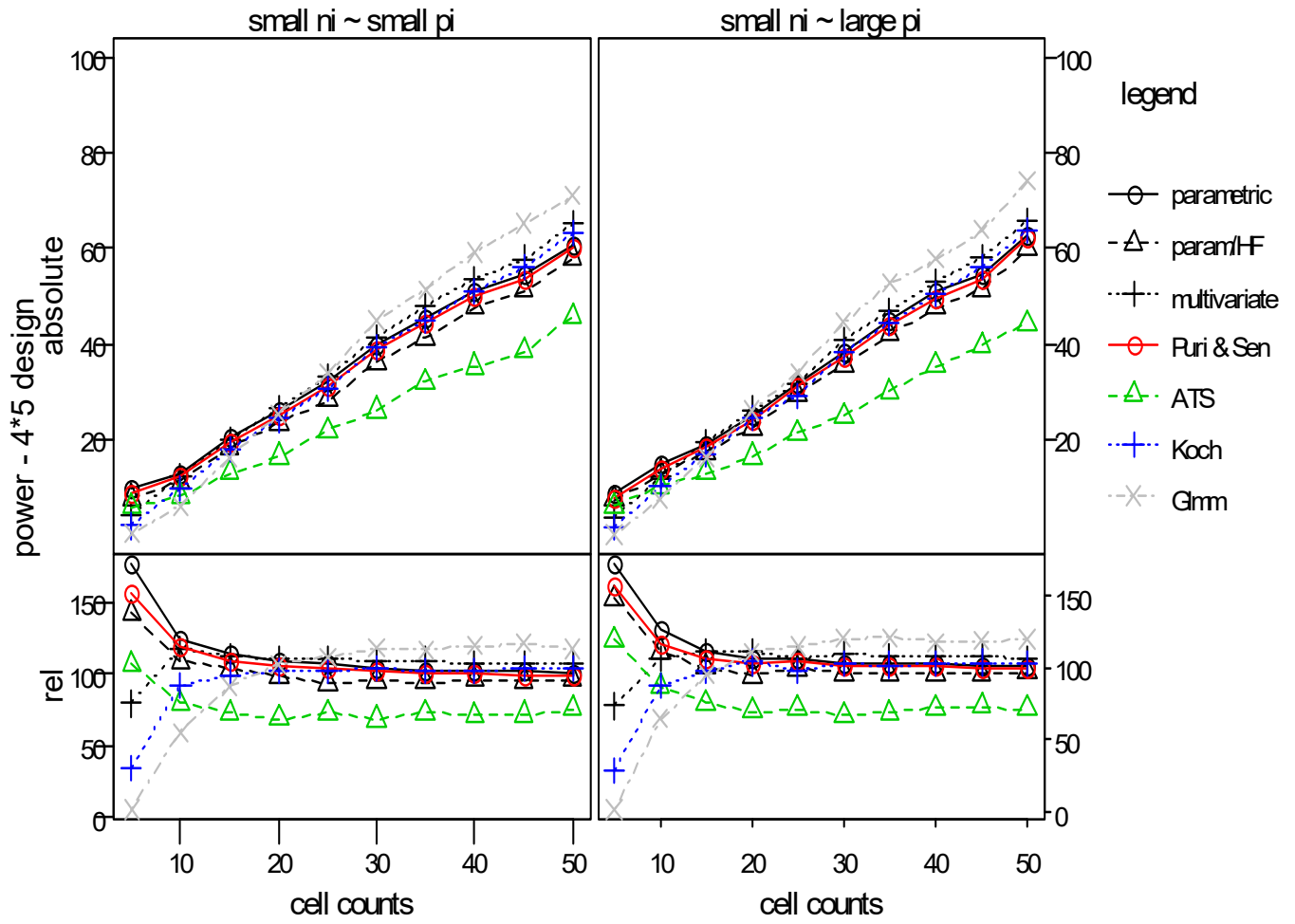
4. 3. 1. 3 $p = 0.9$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	7.05	11.50	16.95	21.55	32.85	42.30	53.05	6.10	9.85	13.70	18.05	27.05	35.45	43.85
	par./ HF-corr.	4.45	9.30	15.25	19.55	31.45	41.85	51.85	4.30	8.70	13.15	17.10	25.95	34.75	43.20
	multivariate	1.15	9.75	17.55	21.50	33.05	42.35	52.65	1.80	10.00	14.20	18.20	26.45	35.65	43.45
	Puri & Sen	5.40	10.65	16.05	20.70	32.10	41.50	52.00	5.35	9.35	13.55	17.55	26.20	35.20	43.50
	ATS	3.45	5.60	9.35	13.85	19.15	24.95	31.95	2.90	5.30	9.60	13.10	21.15	29.45	38.70
	Koch	0.10	6.80	14.55	20.00	31.25	40.40	51.15	0.20	7.95	12.45	16.45	25.45	34.30	42.25
	GLMM	0.10	0.10	0.40	2.00	5.71	10.51	16.32	0.00	0.20	2.10	4.70	12.90	18.60	26.10



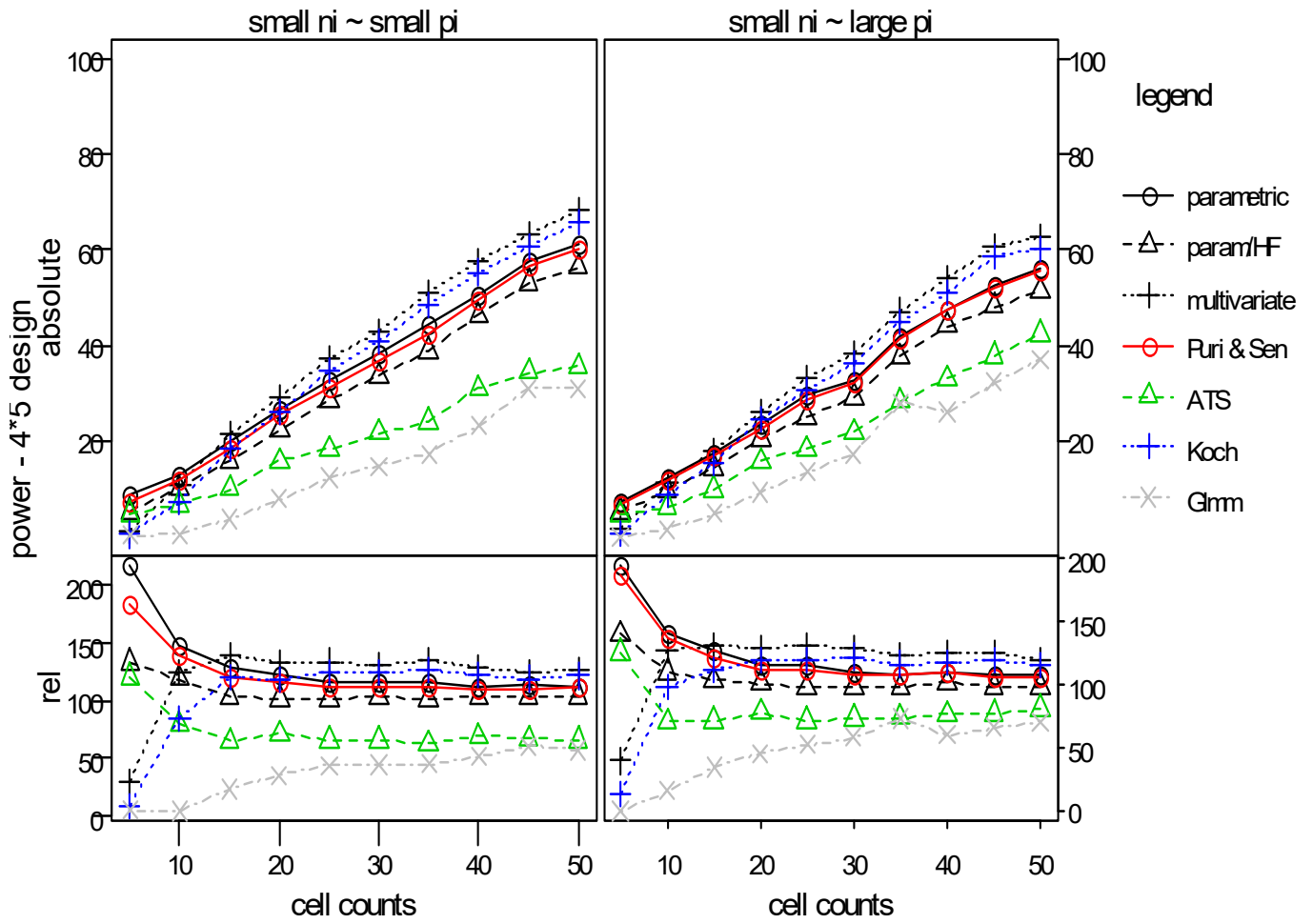
4. 3. 2. unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)**4. 3. 2. 1 $p = 0.5$**

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	9.70	12.90	20.30	25.85	39.65	50.95	60.85	8.65	14.65	19.10	24.95	38.10	50.75	62.50
	par./ HF-corr.	7.80	11.20	18.40	23.30	36.25	47.60	58.15	7.45	13.00	17.20	22.30	35.80	47.60	59.75
	multivariate	4.35	12.15	19.90	26.45	41.15	53.35	65.20	3.70	12.35	19.20	26.25	40.75	53.00	65.75
	Puri & Sen	8.55	12.30	19.30	25.10	38.70	49.85	60.10	7.85	13.60	18.35	24.10	37.25	49.45	61.95
	ATS	5.85	8.25	13.00	16.35	26.00	35.15	45.80	6.00	10.10	13.00	16.40	24.85	35.35	44.25
	Koch	1.90	9.55	17.75	24.25	39.15	50.80	63.05	1.45	10.15	16.85	24.40	38.05	50.55	63.70
	GLMM	0.30	6.10	16.30	25.40	44.80	59.10	71.00	0.10	7.50	16.30	26.00	44.50	57.80	74.00



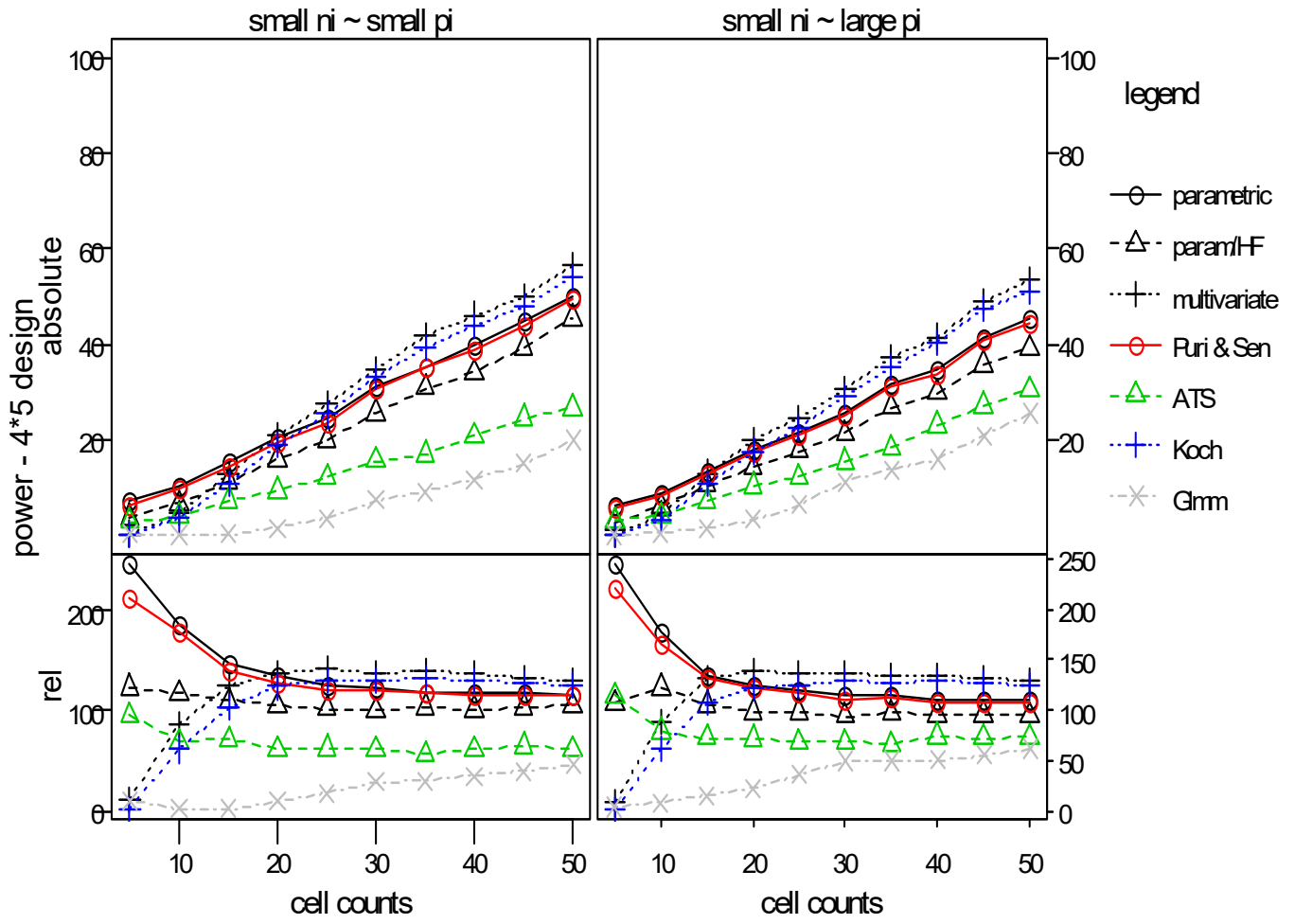
4. 3. 2. 2 $p = 0.8$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	8.55	12.65	19.70	26.65	38.30	50.60	61.10	7.15	12.35	17.55	23.45	32.50	47.50	56.25
	par./ HF-corr.	5.25	10.20	15.75	22.20	33.55	46.30	56.20	5.15	9.60	14.35	20.45	29.10	44.00	51.30
	multivariate	1.20	10.65	21.25	29.10	42.90	57.60	68.20	1.45	11.10	18.05	26.15	38.15	53.75	62.75
	Puri & Sen	7.20	11.85	18.35	25.50	36.90	49.35	60.10	6.85	11.90	16.90	22.60	32.10	47.15	55.45
	ATS	4.75	6.80	9.90	15.60	21.60	30.90	35.55	4.60	6.15	9.85	15.80	21.75	33.00	42.35
	Koch	0.35	7.25	18.50	25.90	40.80	55.25	65.80	0.50	8.55	15.50	24.30	36.20	51.10	60.10
	GLMM	0.20	0.40	3.60	7.81	14.61	23.12	31.03	0.00	1.40	4.80	9.20	17.20	26.00	37.00



4. 3. 2. 3 $p = 0.9$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	7.20	10.35	15.15	20.35	31.35	39.60	50.05	6.30	8.80	13.35	17.85	25.65	34.55	45.20
	par./ HF-corr.	3.60	6.50	11.35	15.85	25.55	34.05	45.40	2.75	6.10	10.45	14.10	21.25	29.80	39.05
	multivariate	0.30	4.85	12.80	20.80	34.65	46.10	56.40	0.20	4.40	13.05	19.75	30.65	41.50	53.30
	Puri & Sen	6.20	9.90	14.45	19.45	30.35	38.90	49.40	5.70	8.25	13.00	17.50	25.05	33.75	44.30
	ATS	2.80	3.85	7.35	9.30	15.55	20.80	26.55	2.95	3.95	7.15	10.25	15.35	23.05	30.35
	Koch	0.05	3.40	10.65	18.80	33.00	44.00	54.05	0.05	3.05	10.70	17.60	29.00	40.10	51.10
	GLMM	0.30	0.10	0.20	1.40	7.40	11.70	19.90	0.10	0.40	1.50	3.30	11.22	15.83	25.55

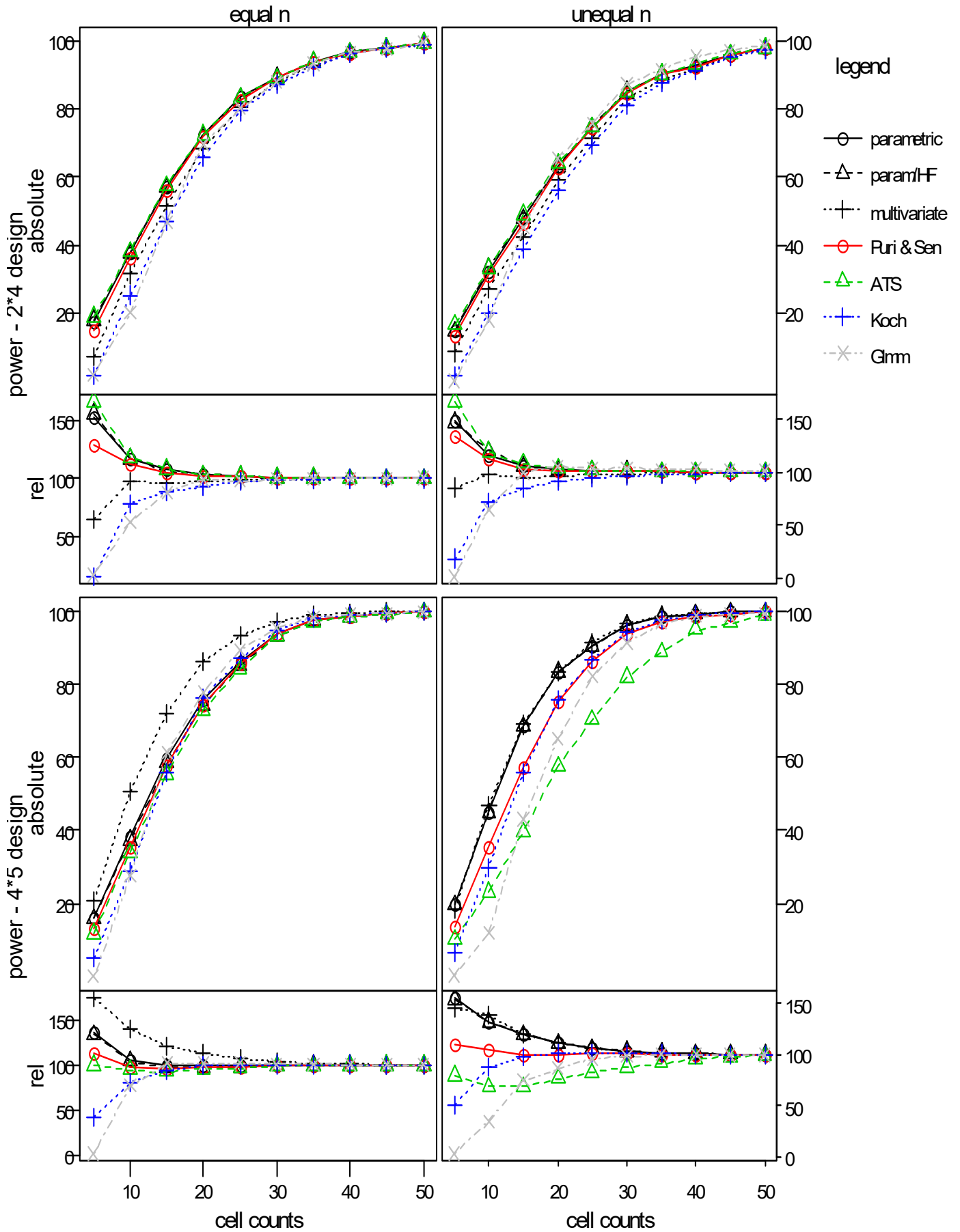


4. 4. Interaction effect AB (effects $ab_{ij} = 0.4*s$)

4. 4. 1. equal correlations on B ($r=0.3$)

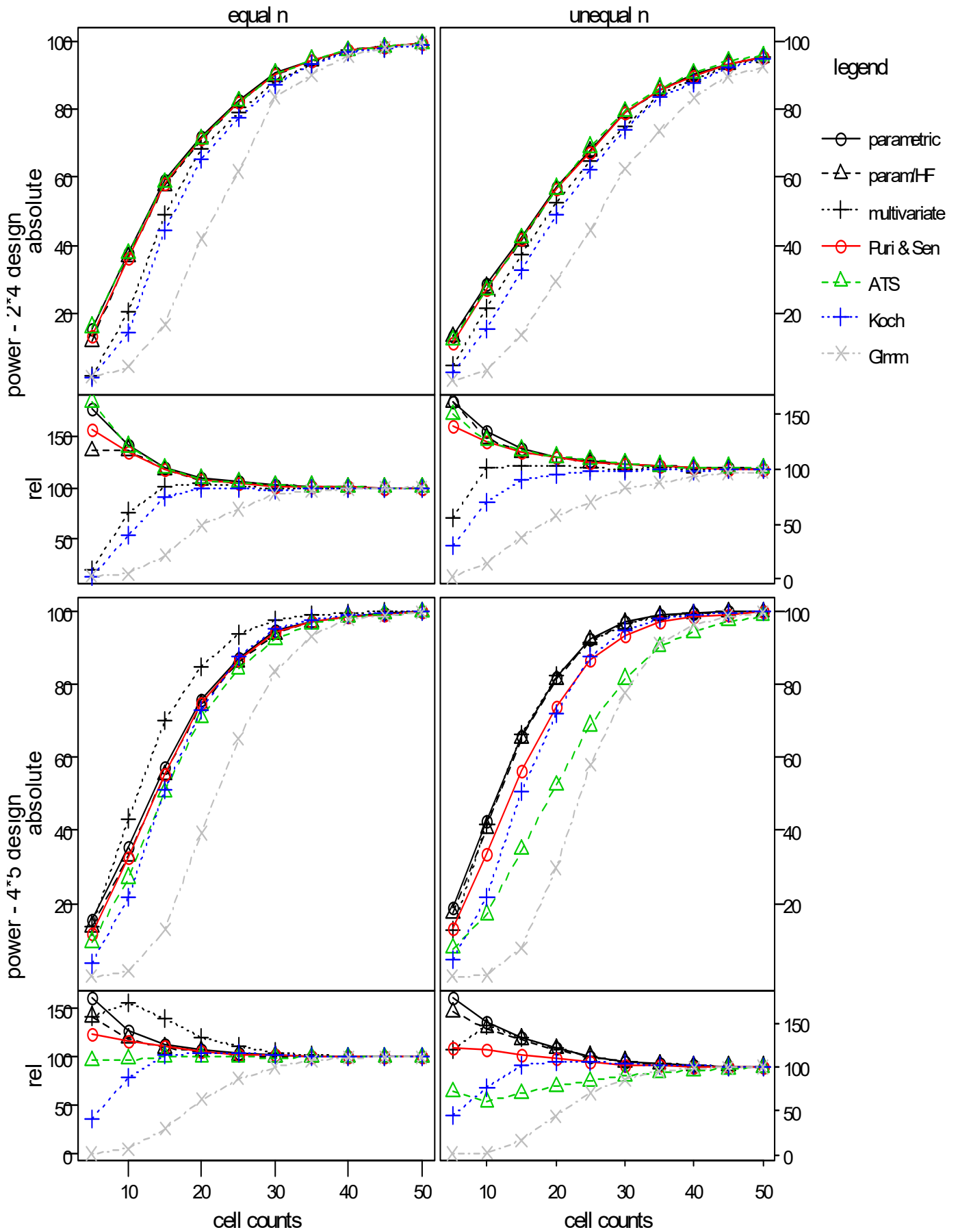
4. 4. 1. 1 $p = 0.5$

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	17.45	37.50	57.05	72.30	89.15	96.60	99.25	14.75	32.20	47.75	63.40	84.80	92.60	97.65
	par./ HF-corr.	17.85	37.65	56.95	72.20	89.05	96.55	99.25	14.65	33.30	47.75	63.40	85.10	92.70	97.70
	multivariate	7.35	31.40	51.30	68.40	87.90	96.45	98.95	8.50	27.00	42.45	59.05	82.90	91.60	97.45
	Puri & Sen	14.80	36.10	56.10	71.60	88.85	96.45	99.20	13.40	31.15	46.45	62.60	84.70	92.40	97.60
	ATS	19.00	38.00	57.50	72.45	89.00	96.55	99.25	16.60	33.15	48.95	63.95	84.80	93.05	97.70
	Koch	1.75	25.25	47.10	65.55	87.25	96.15	98.85	1.80	19.85	38.60	56.25	81.00	91.00	97.30
	GLMM	1.90	20.00	46.70	69.60	88.00	96.50	99.40	0.10	17.90	44.90	65.40	87.30	95.20	98.70
4*5	parametric	16.15	38.15	59.45	75.60	93.85	98.70	99.85	17.75	38.85	58.90	76.15	93.95	98.80	99.80
	par./ HF-corr.	15.80	37.45	58.40	74.20	93.40	98.60	99.80	17.45	37.75	58.05	75.05	93.55	98.70	99.70
	multivariate	20.75	50.60	72.00	86.10	97.35	99.55	99.95	18.30	47.40	69.45	84.10	96.95	99.20	99.90
	Puri & Sen	13.35	35.35	57.65	74.50	93.65	98.65	99.80	13.85	35.70	57.40	75.35	93.80	98.75	99.80
	ATS	11.85	34.00	55.45	72.85	93.15	98.50	99.80	11.25	19.75	32.65	47.35	74.20	90.75	96.80
	Koch	4.95	29.00	55.95	76.20	94.85	99.25	99.90	6.20	30.05	55.50	75.70	94.65	99.30	99.80
	GLMM	0.10	27.60	61.30	77.70	95.40	99.10	99.90	0.40	11.90	43.10	65.20	91.50	98.80	99.40



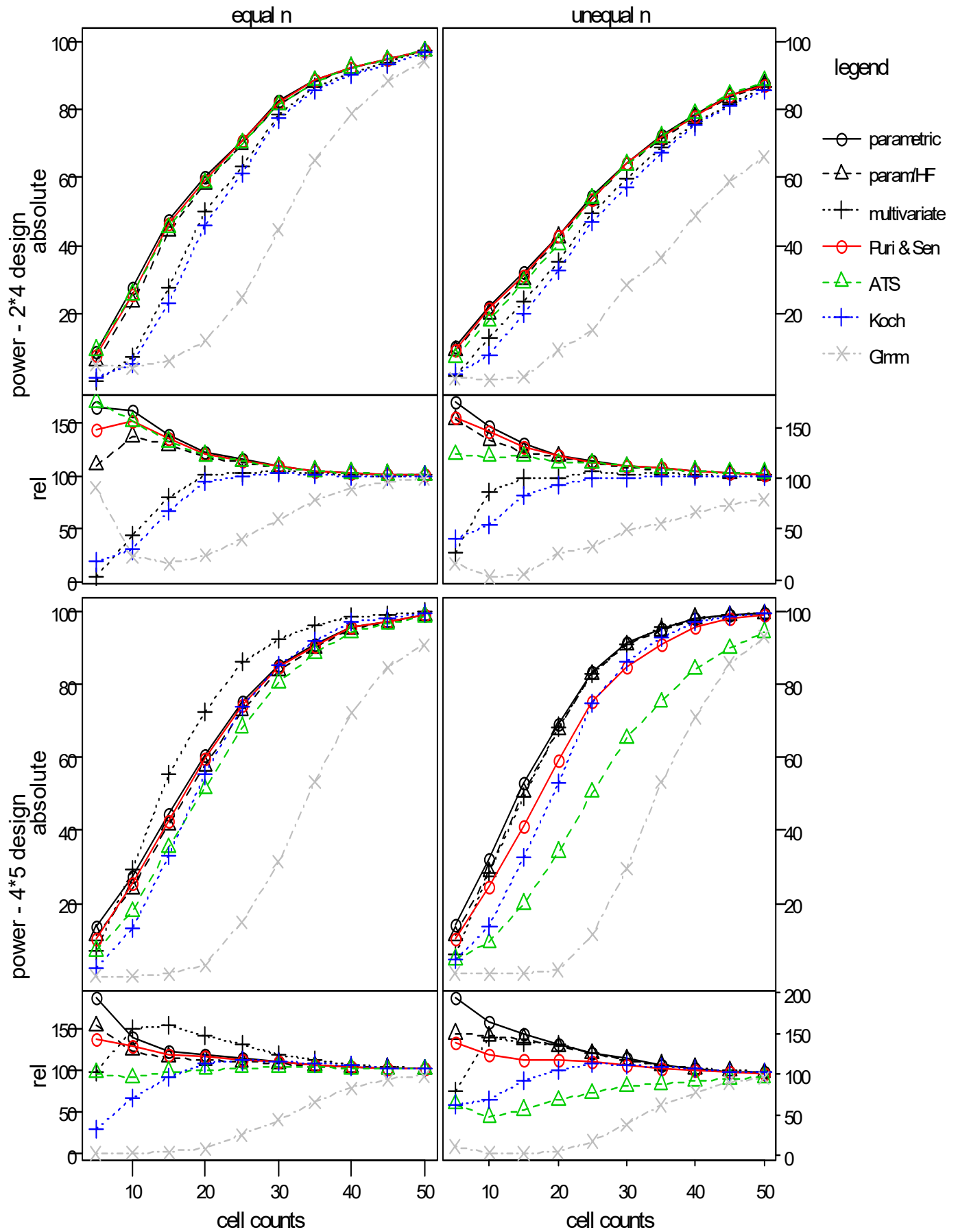
4. 4. 1. 2 p = 0.8

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	15.25	37.95	58.85	71.55	90.45	97.25	99.20	13.10	28.70	42.30	57.05	79.15	89.90	95.05
	par./ HF-corr.	11.75	36.55	57.65	71.00	90.20	97.10	99.15	13.10	27.55	41.40	56.40	78.70	89.70	95.10
	multivariate	1.65	20.45	49.10	68.00	88.20	97.00	98.80	4.50	21.60	37.20	52.35	74.95	88.55	94.95
	Puri & Sen	13.55	36.25	58.20	71.15	89.95	97.15	99.20	11.30	27.00	41.55	56.40	78.90	89.60	94.95
	ATS	15.85	37.50	58.40	71.20	90.25	97.15	99.20	12.15	26.95	42.00	56.65	79.30	90.50	95.50
	Koch	1.15	14.40	44.25	65.05	87.10	96.85	98.80	2.50	15.15	32.55	48.95	73.70	87.70	94.65
	GLMM	1.21	4.33	16.70	41.75	83.50	95.47	99.30	0.20	3.10	13.70	29.50	62.50	83.40	92.30
4*5	parametric	15.65	35.25	57.20	76.00	94.75	98.75	99.90	16.40	36.50	58.10	75.00	93.60	98.60	99.90
	par./ HF-corr.	13.75	32.95	55.20	74.45	93.70	98.65	99.80	14.85	33.75	55.60	73.35	93.00	98.15	99.90
	multivariate	13.70	43.30	70.00	84.70	97.50	99.70	99.95	12.85	40.70	66.60	82.30	96.90	99.45	99.95
	Puri & Sen	11.95	32.40	55.45	74.70	94.25	98.70	99.90	12.95	33.70	56.15	73.70	93.45	98.45	99.90
	ATS	9.35	27.00	50.50	70.90	92.50	98.45	99.75	8.15	14.55	28.30	42.20	72.55	88.20	96.30
	Koch	3.45	21.85	51.20	73.15	95.50	99.20	99.95	4.30	23.30	51.05	73.10	95.40	99.30	99.95
	GLMM	0.00	1.40	12.90	39.30	83.50	97.90	99.90	0.10	0.40	7.90	29.80	77.70	96.30	99.70



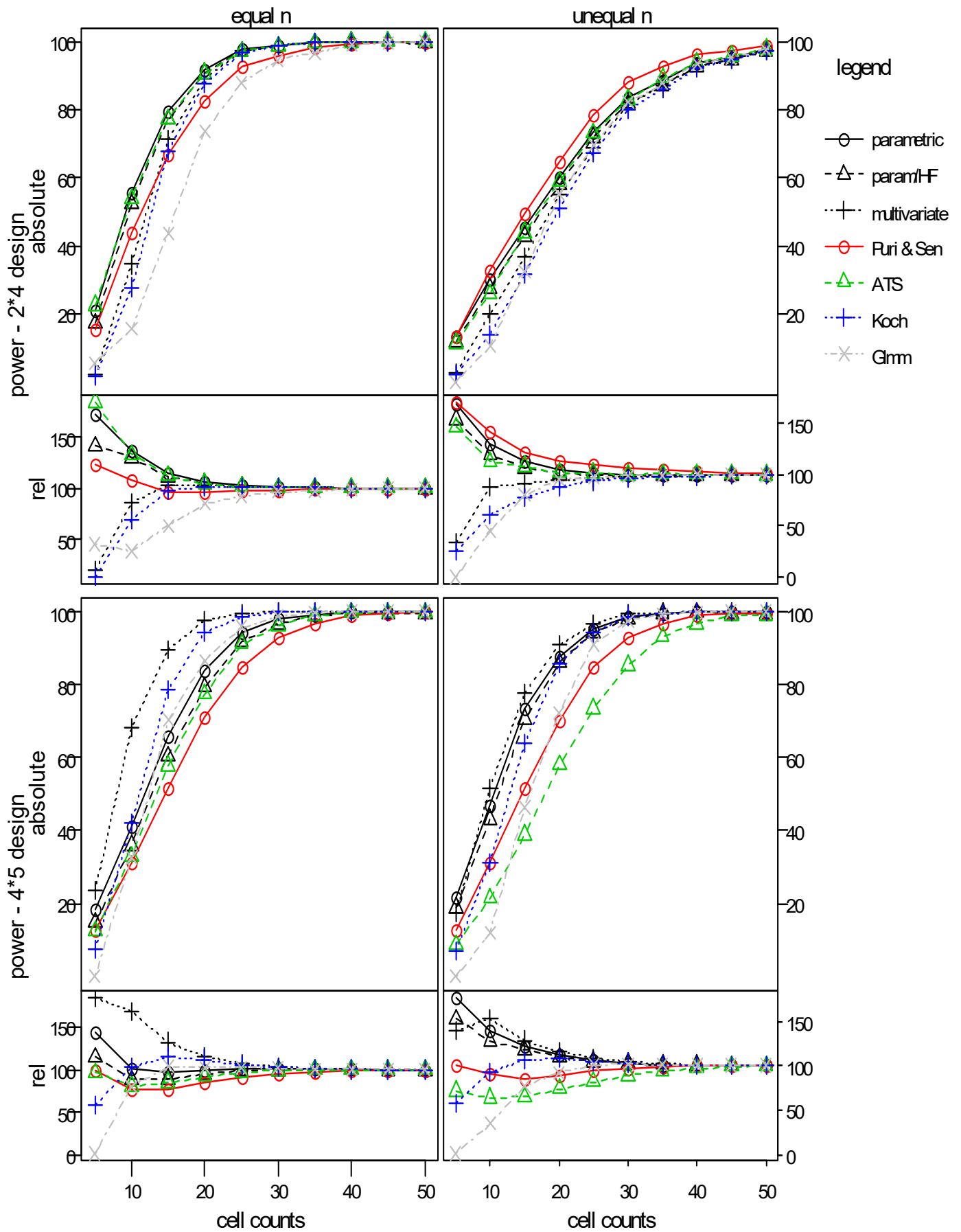
4. 4. 1. 3 p = 0.9

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	8.90	27.35	47.50	59.95	82.30	92.40	97.10	10.15	22.05	32.20	43.00	64.40	78.60	87.55
	par./ HF-corr.	5.95	23.20	44.05	57.95	81.35	92.10	97.10	9.15	20.05	30.00	42.45	63.50	77.80	87.10
	multivariate	0.25	7.40	27.45	49.90	78.40	90.65	97.05	1.55	12.60	23.70	35.30	59.40	76.10	86.30
	Puri & Sen	7.80	25.75	46.30	58.85	81.95	92.20	97.10	9.30	21.30	31.05	42.60	64.05	78.15	87.15
	ATS	9.20	25.60	45.20	58.45	81.40	92.15	97.10	7.15	17.65	29.05	40.25	63.80	78.65	88.25
	Koch	1.00	5.05	22.85	46.05	77.15	89.95	96.90	2.35	7.80	19.85	32.55	57.15	75.15	85.35
	GLMM	4.81	3.99	5.94	11.98	44.52	78.51	94.06	0.90	0.40	1.20	9.20	28.40	48.70	66.10
4*5	parametric	13.80	27.45	44.35	60.60	85.30	95.95	99.00	14.45	28.55	46.20	62.90	88.10	97.05	99.25
	par./ HF-corr.	11.25	24.20	41.45	57.90	83.90	95.15	98.85	11.35	25.60	44.20	61.45	87.00	96.60	99.15
	multivariate	7.20	29.45	55.55	72.45	92.30	98.50	99.95	7.25	28.00	51.70	69.50	90.75	97.75	99.65
	Puri & Sen	10.15	25.30	42.55	59.70	84.80	95.90	99.00	10.30	24.35	41.40	59.25	84.95	95.95	99.15
	ATS	7.10	17.85	35.35	51.55	80.65	94.20	98.60	6.00	8.35	17.85	29.25	57.70	79.55	91.80
	Koch	2.20	13.15	33.15	55.20	85.45	97.10	99.45	4.50	14.20	32.35	53.55	85.80	97.20	99.35
	GLMM	0.00	0.10	0.60	3.00	31.40	72.10	90.90	0.80	0.60	0.80	1.81	29.38	71.03	92.96



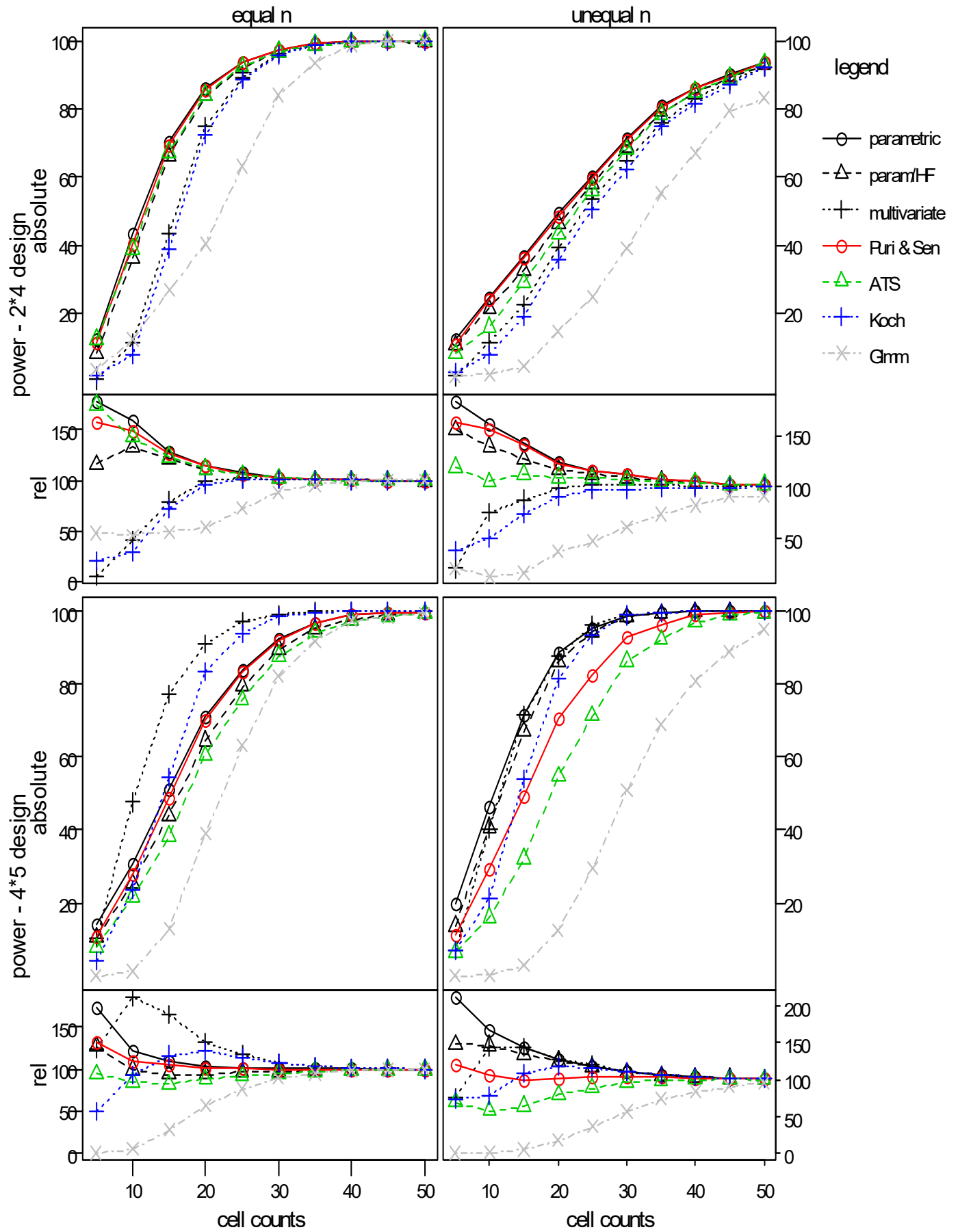
4. 4. 2. unequal correlations on B (r = 0.7, 0.5, 0.4, 0.2)**4. 4. 2. 1 p = 0.5**

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	21.15	55.75	79.20	91.55	98.80	99.95	99.95	13.10	29.95	45.40	60.10	83.30	93.50	97.55
	par./ HF-corr.	17.30	52.40	77.10	90.60	98.65	99.95	99.95	11.90	27.60	42.80	58.20	81.90	92.60	97.20
	multivariate	2.35	34.45	71.45	89.20	98.70	99.95	99.95	2.60	20.05	36.80	54.90	81.40	92.55	97.20
	Puri & Sen	15.10	43.65	66.80	82.45	95.85	99.45	99.95	13.20	32.65	49.30	64.75	87.90	96.00	99.00
	ATS	22.55	53.85	77.25	90.65	98.65	99.90	99.95	11.35	25.85	43.80	58.85	82.95	93.80	97.85
	Koch	1.55	27.80	67.70	87.60	98.60	99.90	99.95	1.95	14.00	31.60	50.90	79.90	92.20	97.05
	GLMM	5.50	15.40	43.60	73.50	94.50	99.00	100.0	0.00	10.40	32.30	55.10	82.20	93.50	97.50
4*5	parametric	18.55	41.05	65.85	83.70	98.15	99.90	99.95	19.25	42.10	66.05	85.05	98.05	99.80	99.95
	par./ HF-corr.	14.75	35.95	60.45	79.30	96.50	99.75	99.95	16.05	37.00	60.45	79.40	97.20	99.60	99.90
	multivariate	23.75	68.25	89.75	97.45	99.95	99.95	99.95	23.10	64.20	86.75	97.05	99.95	99.95	99.95
	Puri & Sen	12.70	31.30	51.60	70.85	92.90	99.00	99.85	12.50	31.00	51.60	70.10	92.95	99.05	99.75
	ATS	12.45	33.00	57.75	77.45	96.05	99.75	99.95	12.35	20.35	34.00	49.50	79.55	94.55	98.80
	Koch	7.60	42.10	78.60	94.45	99.90	99.95	99.95	9.00	42.25	78.70	94.15	99.85	99.95	99.95
	GLMM	0.20	32.60	70.30	86.50	98.80	100.0	100.0	0.10	11.80	46.40	72.40	97.60	99.90	100.00



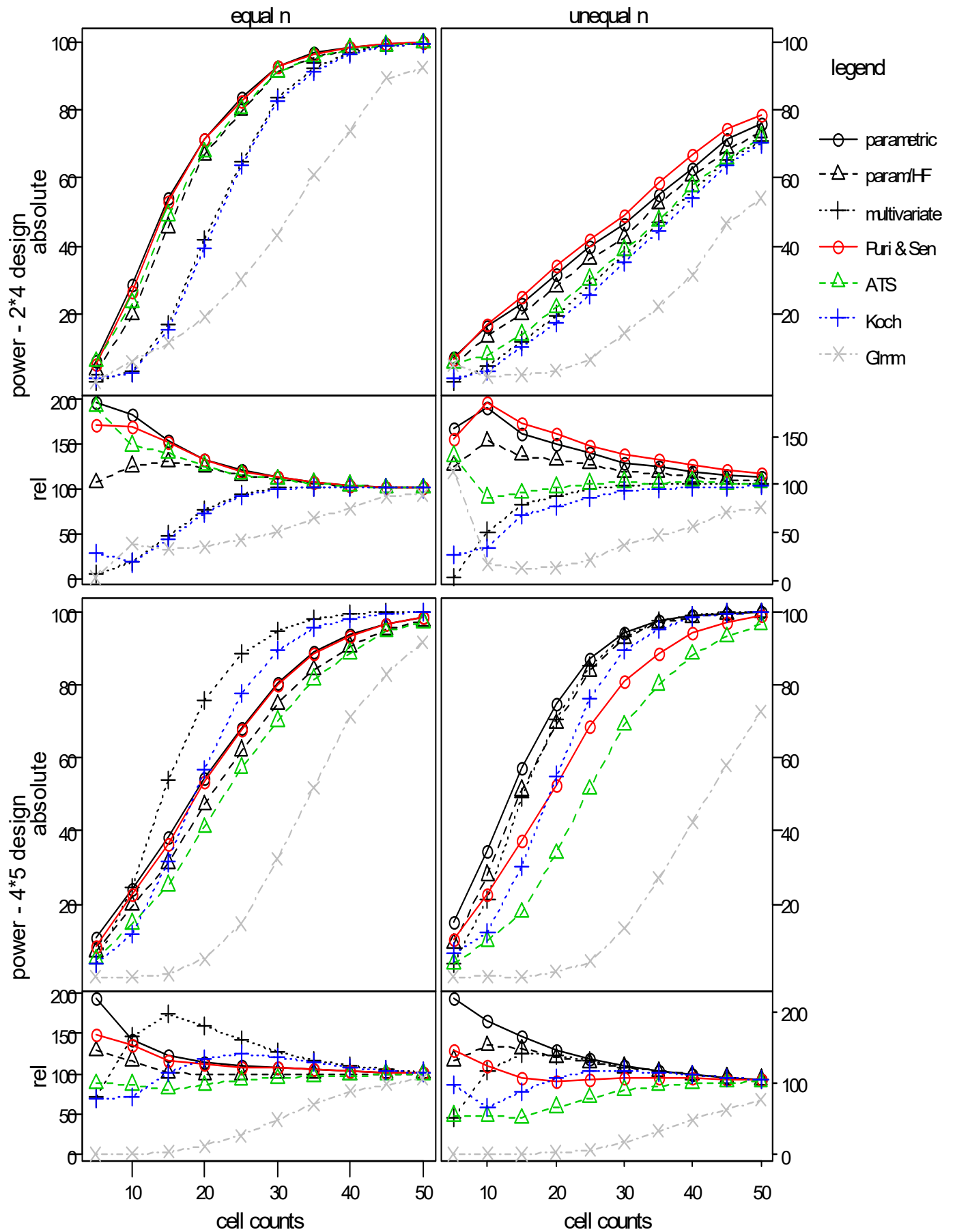
4. 4. 2. 2 $p = 0.8$

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	12.50	43.30	70.30	86.00	97.25	99.60	99.95	12.40	24.70	36.60	49.25	71.45	86.25	93.65
	par./ HF-corr.	8.15	36.05	66.10	83.75	96.85	99.55	99.95	10.55	21.30	32.50	46.10	68.90	84.50	92.85
	multivariate	0.35	11.25	43.30	74.95	96.30	99.65	99.95	1.40	11.50	22.55	39.10	64.55	82.80	92.30
	Puri & Sen	11.05	40.45	69.35	85.75	97.15	99.60	99.95	11.00	23.80	36.05	48.40	71.00	85.95	93.55
	ATS	12.30	38.70	67.30	84.05	96.80	99.50	99.95	8.10	16.00	28.85	43.20	68.05	85.00	93.55
	Koch	1.45	7.70	38.95	72.20	95.90	99.55	99.95	2.60	7.60	18.80	35.85	62.10	81.60	92.10
	GLMM	3.34	12.25	26.62	40.28	84.01	98.58	100.0	1.41	2.02	4.23	14.62	39.01	67.14	83.06
4*5	parametric	14.35	30.90	51.00	71.20	92.60	99.05	99.70	14.55	31.50	50.30	71.65	93.05	99.00	99.80
	par./ HF-corr.	10.55	25.35	43.90	64.50	89.55	97.75	99.50	11.25	26.65	43.80	63.75	90.00	98.05	99.75
	multivariate	10.35	47.60	77.10	91.10	99.20	99.95	99.95	9.85	42.15	73.65	88.70	98.90	99.90	99.95
	Puri & Sen	10.95	28.00	49.00	70.10	92.05	98.90	99.70	11.30	29.35	49.10	70.60	92.80	98.95	99.80
	ATS	7.85	21.70	38.40	60.40	87.70	97.35	99.50	7.10	13.10	21.20	33.60	63.90	84.90	95.20
	Koch	4.10	23.75	54.55	83.50	98.75	99.95	99.95	6.15	24.40	53.85	82.55	98.80	99.95	99.95
	GLMM	0.00	1.30	12.80	39.00	82.20	97.40	99.40	0.05	0.30	2.80	12.50	50.80	80.90	95.00



4. 4. 2. 3 p = 0.9

design	method	equal cell counts							unequal cell counts						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
2*4	parametric	6.15	28.45	53.85	71.30	92.90	98.50	99.80	7.10	16.45	23.10	31.70	46.30	62.85	75.90
	par./ HF-corr.	3.35	19.60	45.35	66.55	91.10	97.85	99.70	5.35	13.20	19.70	28.00	42.45	60.35	73.45
	multivariate	0.15	2.90	17.00	41.60	83.55	96.90	99.40	0.20	4.70	12.00	19.65	37.05	55.80	71.00
	Puri & Sen	5.35	26.40	52.85	71.10	92.75	98.35	99.80	6.60	16.85	24.80	34.20	49.10	66.95	78.60
	ATS	6.00	23.20	49.05	67.55	91.25	97.80	99.70	5.80	7.90	13.80	21.75	38.70	57.60	71.95
	Koch	0.90	2.80	15.15	39.40	82.70	96.45	99.50	1.20	3.10	10.40	17.45	35.35	54.15	70.05
	GLMM	0.05	6.09	11.37	18.98	43.25	73.60	92.28	5.07	1.62	2.13	3.22	14.29	31.49	54.02
4*5	parametric	10.65	24.00	38.20	54.35	80.40	93.65	98.55	12.80	25.75	41.85	57.00	84.05	95.60	99.45
	par./ HF-corr.	7.05	19.55	31.25	47.25	74.75	90.50	97.50	8.60	20.95	35.10	51.15	79.40	93.35	98.70
	multivariate	3.85	24.45	54.15	75.70	94.85	99.45	99.95	4.55	24.15	50.15	70.60	92.60	99.00	99.95
	Puri & Sen	8.20	22.75	36.30	53.65	79.90	93.45	98.55	10.10	22.60	37.40	52.75	80.95	94.15	98.95
	ATS	4.80	14.55	25.05	40.95	70.15	88.65	97.25	4.25	7.70	13.75	22.80	48.20	69.55	87.65
	Koch	3.80	11.80	31.45	56.75	89.55	98.10	99.85	5.65	14.25	31.15	55.90	90.20	98.70	99.95
	GLMM	0.00	0.10	0.80	4.90	32.40	71.30	91.80	0.05	0.20	0.10	1.50	13.31	42.54	72.87

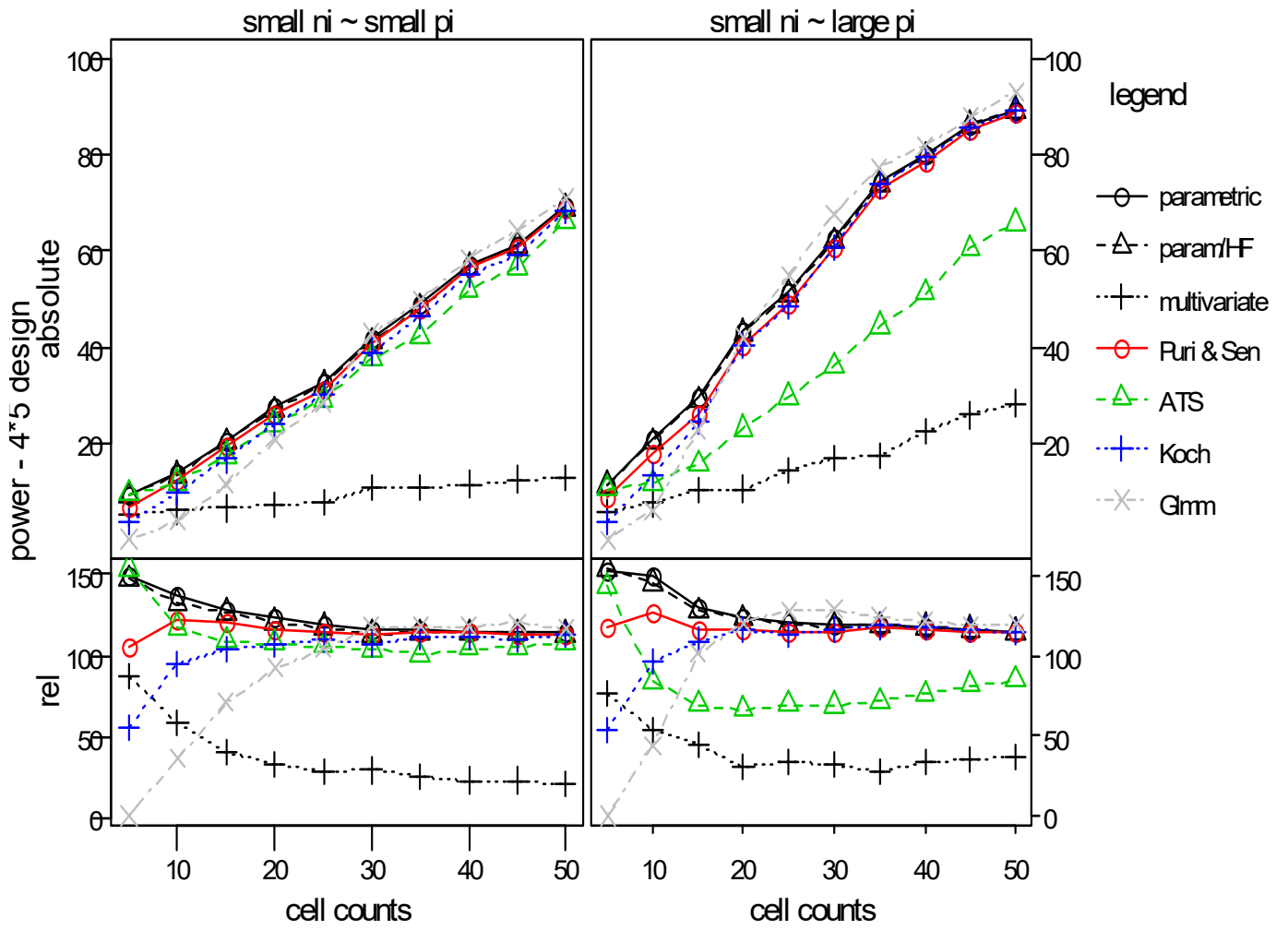


4. 5. Interaction effect AB (effects $ab_i = 0.4*s$)
A significant (effects $a_i = 0.4*s$)
small $n_i \sim$ small p_i and small $n_i \sim$ large p_i

4. 5. 1. equal correlations on B (r=0.3)

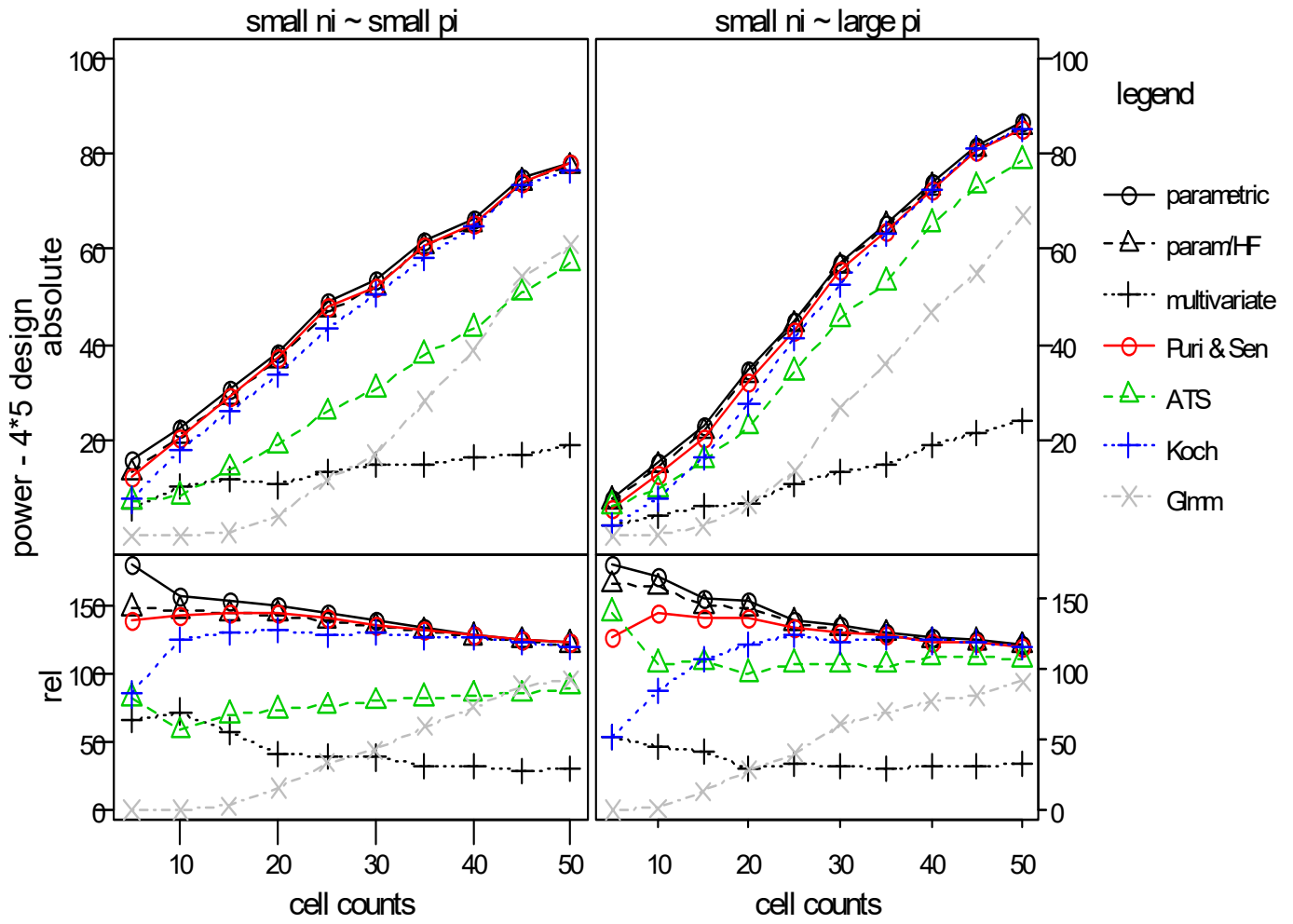
4. 5. 1. 1 p = 0.5

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	9.15	13.85	20.45	27.50	41.90	56.90	69.35	11.15	20.85	29.35	43.15	62.45	79.70	89.20
	par./ HF-corr.	9.05	13.45	20.30	26.95	41.10	56.60	68.85	11.25	20.35	28.85	42.80	62.00	79.60	89.15
	multivariate	5.35	5.95	6.45	7.40	10.70	11.50	12.90	5.60	7.50	10.05	10.50	16.70	22.30	28.30
	Puri & Sen	6.50	12.30	19.35	25.95	41.00	56.55	68.85	8.60	17.65	26.25	40.40	60.40	78.60	88.60
	ATS	9.45	11.90	17.45	24.05	37.80	51.75	66.10	10.45	11.65	15.65	23.00	36.10	51.20	65.70
	Koch	3.45	9.65	16.65	24.05	38.95	55.00	68.45	3.85	13.45	24.65	40.40	60.65	79.25	89.05
	GLMM	0.10	3.70	11.40	20.70	42.80	58.40	70.80	0.00	6.10	22.80	41.80	67.60	81.90	93.00



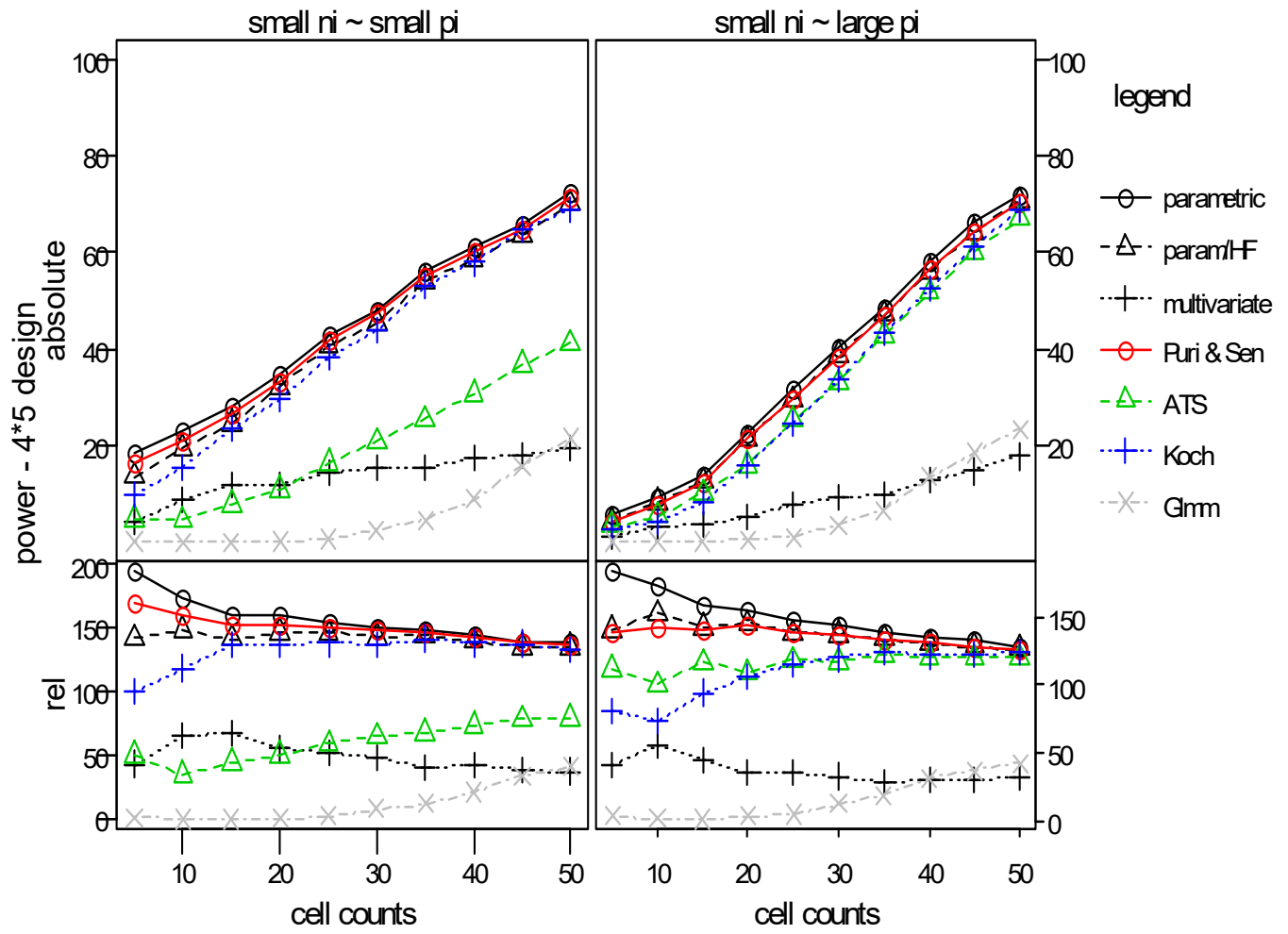
4. 5. 1. 2 p = 0.8

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	15.95	22.55	30.65	38.45	53.50	66.05	78.10	7.85	15.20	22.80	34.90	57.25	73.70	86.35
	par./ HF-corr.	13.15	20.90	28.90	36.75	51.85	64.90	77.15	7.20	14.55	21.85	33.50	56.35	72.80	85.45
	multivariate	5.85	10.30	11.60	10.55	14.75	16.55	18.95	2.30	4.05	6.25	6.75	13.35	18.75	24.00
	Puri & Sen	12.35	20.35	29.00	37.10	52.15	65.40	77.75	5.50	12.85	20.60	32.15	55.35	72.35	85.10
	ATS	7.30	8.30	14.05	18.85	30.75	43.30	57.20	6.30	9.50	15.90	22.65	45.35	65.20	78.55
	Koch	7.50	17.80	26.10	33.90	50.25	64.70	76.25	2.30	7.80	16.30	27.45	52.35	72.50	85.20
	GLMM	0.00	0.00	0.60	4.10	16.90	38.70	60.80	0.00	0.10	2.00	6.50	26.60	46.70	66.80



4. 5. 1. 3 p = 0.9

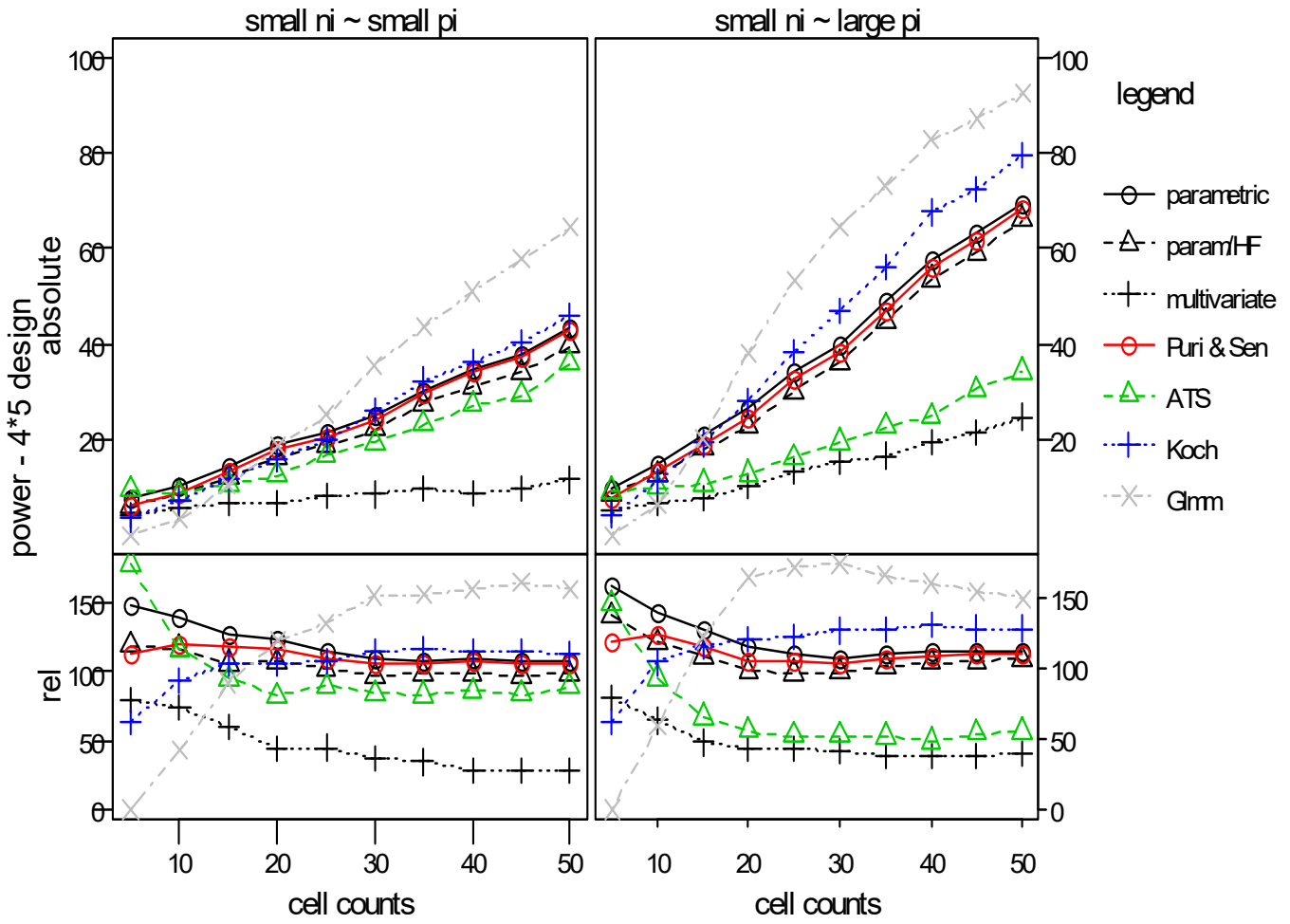
design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	18.50	22.85	27.95	34.60	48.15	60.95	72.25	5.50	9.35	13.95	22.70	40.45	58.20	71.60
	par./ HF-corr.	13.50	19.55	24.60	31.90	45.45	58.65	69.95	4.20	8.20	12.50	21.35	38.75	56.10	70.60
	multivariate	4.10	8.60	11.75	11.95	15.50	17.45	19.35	1.20	2.95	3.85	5.20	9.20	12.70	17.65
	Puri & Sen	16.20	21.10	26.30	33.30	47.25	60.15	71.05	4.15	7.65	12.30	21.20	38.35	56.55	70.50
	ATS	4.75	4.55	7.70	10.90	20.75	30.70	41.15	3.35	5.40	10.20	16.00	33.05	51.65	66.95
	Koch	9.55	15.55	23.65	29.75	43.75	57.85	68.85	2.40	3.95	8.25	15.65	33.75	52.35	68.90
	GLMM	0.10	0.00	0.00	0.10	2.50	8.80	21.40	0.10	0.10	0.10	0.50	3.50	13.41	23.32



4. 5. 2. unequal correlations on B ($r = 0.7, 0.5, 0.4, 0.2$)

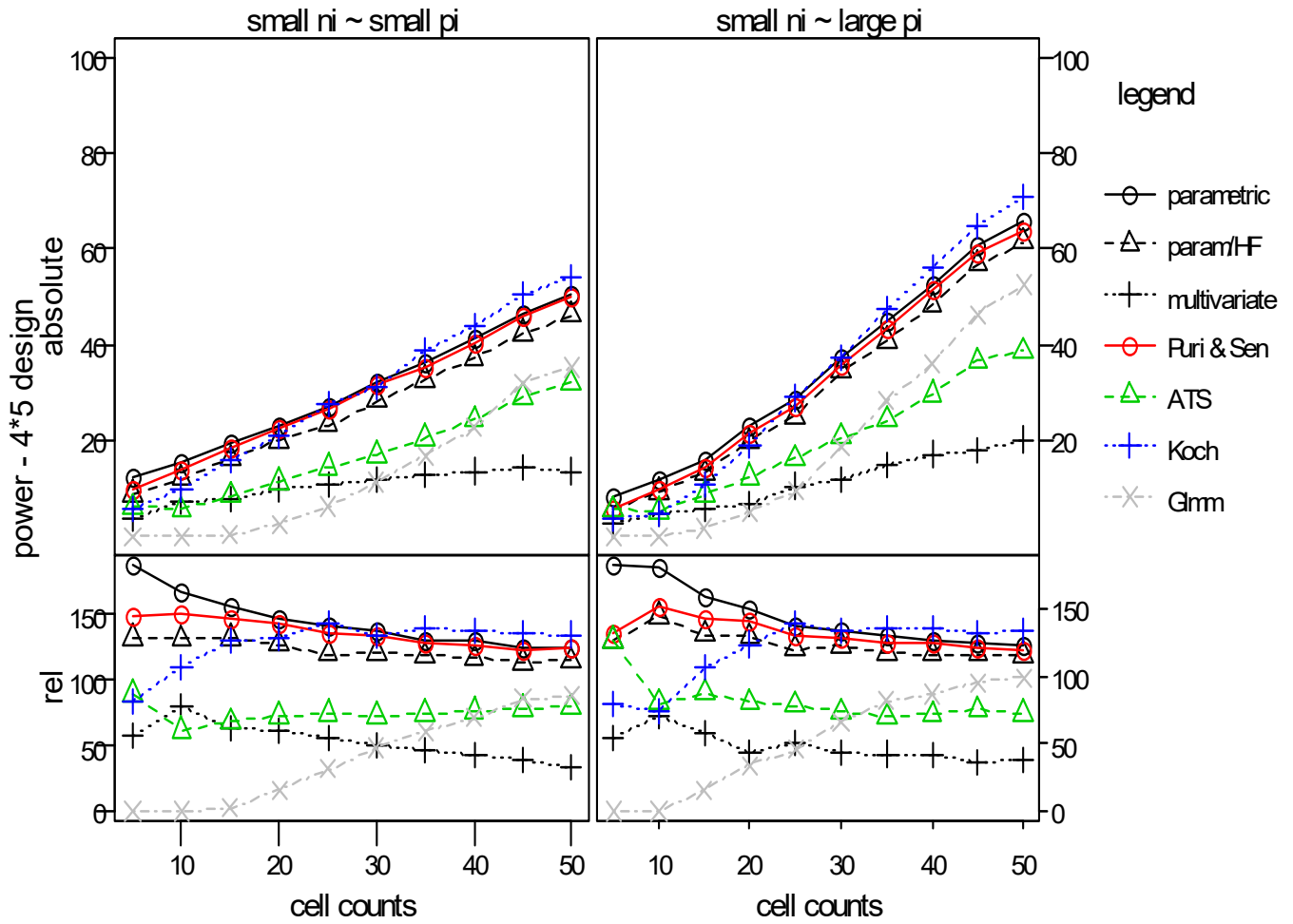
4. 5. 2. 1 $p = 0.5$

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	7.90	10.45	14.40	18.70	25.15	34.65	43.15	10.00	14.90	21.05	26.60	39.65	57.45	69.50
	par./ HF-corr.	6.30	8.70	12.00	16.25	22.20	31.20	39.50	8.70	12.60	18.10	22.65	36.05	53.60	65.95
	multivariate	4.20	5.50	6.70	6.75	8.50	8.90	11.55	5.00	6.70	7.85	10.10	15.35	19.35	24.75
	Puri & Sen	6.00	8.90	13.35	17.70	24.15	33.95	42.80	7.50	13.15	19.10	24.35	38.45	56.25	68.40
	ATS	9.45	8.65	10.70	12.50	19.25	27.25	35.85	9.20	9.95	10.90	12.90	19.40	24.95	34.20
	Koch	3.40	7.00	11.95	16.10	26.20	36.20	45.75	3.95	11.10	19.20	27.90	47.05	67.50	79.45
	GLMM	0.00	3.20	10.40	18.60	35.60	50.90	64.40	0.00	6.30	20.30	38.10	64.60	82.70	92.40



4. 5. 2. 2 p = 0.8

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	12.45	15.15	19.40	23.05	32.15	41.30	50.25	8.05	11.60	16.10	22.80	37.40	52.65	65.75
	par./ HF-corr.	8.75	11.95	16.30	19.95	28.30	37.10	46.05	5.60	9.30	13.25	19.75	34.35	48.35	61.35
	multivariate	3.85	7.25	7.75	9.65	11.85	13.55	13.55	2.40	4.50	5.90	6.65	11.95	17.10	20.15
	Puri & Sen	9.90	13.70	18.15	22.40	31.45	40.40	49.70	5.80	9.75	14.50	21.50	35.85	51.40	63.50
	ATS	5.95	5.60	8.45	11.35	17.00	24.30	31.90	5.60	5.15	8.85	12.30	20.60	29.60	38.50
	Koch	5.50	9.95	16.05	20.85	31.30	44.00	54.05	3.50	4.80	10.80	18.85	37.35	56.10	70.95
	GLMM	0.00	0.00	0.30	2.50	11.30	22.70	35.20	0.00	0.00	1.60	5.10	18.60	36.00	52.50



4. 5. 2. 3 p = 0.9

design	method	unequal cell counts small $n_i \sim$ small p_i							unequal cell counts small $n_i \sim$ large p_i						
		5	10	15	20	30	40	50	5	10	15	20	30	40	50
4*5	parametric	14.15	15.00	18.90	22.95	29.45	37.45	44.35	7.50	8.55	12.30	17.05	27.75	40.70	49.85
	par./ HF-corr.	9.00	11.45	14.05	18.95	25.95	32.35	39.75	4.15	6.50	9.60	14.00	24.45	36.35	45.15
	multivariate	2.05	5.45	8.35	9.15	10.65	13.00	13.50	1.05	3.10	4.55	5.85	9.10	11.70	13.70
	Puri & Sen	11.70	13.90	17.70	21.70	28.75	36.75	43.75	6.00	7.65	11.10	15.85	26.50	39.80	48.20
	ATS	3.70	2.95	4.55	8.30	12.30	16.80	22.25	2.50	2.85	5.75	7.85	14.95	23.90	30.70
	Koch	7.30	11.60	14.25	19.95	29.15	38.40	47.35	4.20	3.40	5.25	10.30	24.60	39.00	51.70
	GLMM	0.10	0.00	0.00	0.20	1.40	9.90	15.80	0.00	0.00	0.00	0.10	3.60	12.30	19.80

