

Comparison of nonparametric analysis of variance methods - a Monte Carlo study

Part A: Two between subjects factors designs

Appendix 1 Tables and Graphs of the Type I Error Rates

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1. 1 equal means - equal cell counts

Table 1-1-1a:
equal means - $n_i=10$ - n of levels=2*4 - $\alpha=0.05$

distribution type	effect	param	RT	INT	ART	ART+INT	Puri & Sen	van der Waerden	ATS
normal equal variances	A	5.54	5.50	5.48	5.30	5.56	5.46	5.54	5.48
	B	4.58	4.62	4.72	4.74	4.56	4.32	4.46	4.34
	AB	4.50	4.96	4.70	5.10	4.84	4.46	4.46	4.74
normal unequal variances (on B)	A	5.68	5.34	5.58	6.98	6.24	5.20	5.44	5.28
	B	6.44	6.00	5.52	5.80	5.36	5.56	5.20	5.20
	AB	5.86	4.82	5.28	6.34	5.92	4.60	5.02	4.58
normal unequal variances (on A and B)	A	5.76	5.30	5.52	6.80	6.12	5.12	5.38	5.26
	B	5.94	5.80	5.40	6.12	5.56	5.46	5.08	5.24
	AB	5.62	5.06	5.02	6.52	5.70	4.56	4.62	4.60
right skewed	A	5.00	5.40	5.22	5.42	4.82	5.18	5.20	5.36
	B	4.72	4.92	4.94	5.06	4.28	4.66	4.62	4.82
	AB	5.08	5.28	5.02	5.56	5.28	5.06	4.74	5.06
exponential continuous	A	4.34	4.74	4.66	5.18	4.24	4.70	4.70	4.72
	B	4.76	5.44	5.32	5.52	4.14	4.98	4.66	5.18
	AB	4.68	5.66	5.32	6.12	5.42	5.22	4.92	5.32
exponential discrete	A	4.46	4.84	4.74	5.86	4.52	4.76	4.60	4.80
	B	4.60	5.20	5.26	5.92	3.92	4.90	4.94	5.08
	AB	4.54	5.54	5.28	6.58	5.54	5.08	4.86	5.38
lognormal (0 / 0.25)	A	5.04	4.98	5.00	5.26	4.82	5.08	5.08	4.94
	B	4.56	4.90	4.92	4.86	4.66	4.68	4.66	4.86
	AB	4.46	4.88	4.86	4.82	4.78	4.62	4.44	4.54
uniform continuous	A	5.38	5.40	5.22	4.94	5.10	5.18	5.20	5.36
	B	4.90	4.92	4.94	4.96	4.84	4.66	4.62	4.82
	AB	5.18	5.28	5.02	5.34	5.08	5.06	4.74	5.06
uniform discrete	A	5.12	5.06	5.08	5.94	5.80	4.98	5.02	5.02
	B	4.90	4.82	4.70	4.80	4.30	4.48	4.48	4.62
	AB	4.82	4.82	4.92	4.94	4.72	4.56	4.68	4.70
left/right skewed	A	5.12	4.18	7.02	4.34	4.44	4.12	6.66	4.16
	B	5.16	5.12	5.20	4.42	5.20	4.90	4.96	5.00
	AB	4.76	4.78	4.82	4.86	4.76	4.48	4.40	4.48
left skewed unequalvariances (on B)	A	5.12	5.08	5.04	7.12	5.52	4.88	5.02	4.98
	B	5.40	5.38	4.58	5.24	4.56	5.14	4.32	4.84
	AB	6.26	5.54	6.42	6.70	6.66	5.18	5.98	5.22
left skewed unequalvariances (on A and B)	A	5.16	5.20	4.96	7.24	5.74	4.90	4.70	5.08
	B	5.36	5.24	5.06	5.50	5.20	4.92	4.78	4.72
	AB	5.92	5.60	6.02	6.72	6.38	5.08	5.58	5.32

Table 1-1-1b:
equal means - $n_i=10$ - n of levels=2*4 - $\alpha=0.01$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	A	0.92	1.02	0.94	1.16	1.14	0.90	0.78	1.00
	B	0.94	1.12	1.00	0.64	0.74	0.94	0.80	1.08
	AB	1.22	1.32	1.38	1.10	0.92	1.10	1.16	1.16
normal unequal variances (on B)	A	0.76	0.94	0.86	1.78	1.42	0.76	0.72	1.00
	B	1.74	1.36	1.32	1.12	1.30	1.28	1.14	1.26
	AB	1.78	1.22	1.52	1.48	1.60	1.14	1.38	1.18
normal unequal variances (on A and B)	A	1.08	1.02	0.96	1.58	1.24	0.94	0.94	0.96
	B	1.48	1.10	1.10	1.18	1.14	0.94	0.88	0.88
	AB	1.54	1.22	1.32	1.54	1.52	1.14	1.12	1.18
right skewed	A	0.86	0.98	0.82	0.94	0.70	0.70	0.66	0.92
	B	1.04	0.78	0.86	0.92	0.72	0.62	0.66	0.68
	AB	1.16	1.24	1.12	1.14	1.10	1.00	0.84	1.06
exponential continuous	A	0.88	0.96	1.00	1.14	0.76	0.88	0.90	0.96
	B	0.70	0.94	0.86	0.94	0.74	0.76	0.70	0.84
	AB	0.88	1.20	1.16	1.58	1.24	0.84	0.92	1.06
exponential discrete	A	0.84	0.84	0.98	1.22	0.90	0.82	0.88	0.84
	B	0.86	1.06	1.00	1.10	0.58	0.88	0.74	0.94
	AB	0.88	1.24	1.00	1.64	1.42	1.00	0.90	1.20
lognormal (0 / 0.25)	A	1.22	1.12	1.2	1.28	1.22	1.04	1.14	1.12
	B	1.04	1.30	1.3	1.32	1.24	0.96	1.06	1.22
	AB	0.86	0.88	0.9	0.90	0.90	0.70	0.62	0.74
uniform continuous	A	0.88	0.98	0.82	0.94	0.98	0.70	0.66	0.92
	B	0.76	0.78	0.86	0.78	0.94	0.62	0.66	0.68
	AB	1.00	1.24	1.12	1.18	0.98	1.00	0.84	1.06
uniform discrete	A	0.90	0.94	0.98	1.08	1.14	0.80	0.80	0.94
	B	0.82	0.82	0.80	0.86	0.80	0.62	0.60	0.70
	AB	1.04	1.16	1.10	1.20	1.08	0.88	0.86	1.06
left/right skewed	A	1.10	1.14	1.06	1.18	1.06	1.14	1.04	1.14
	B	0.78	0.84	1.06	0.84	0.96	0.70	0.86	0.76
	AB	1.24	1.24	1.18	1.32	1.18	0.96	0.80	1.14
left skewed unequal variances (on B)	A	1.04	1.16	1.10	1.88	1.06	0.96	0.88	1.14
	B	1.54	1.10	1.10	1.18	1.20	0.92	0.98	0.86
	AB	1.92	1.44	1.88	1.78	1.92	1.24	1.60	1.30
left skewed unequal variances (on A and B)	A	0.92	1.08	0.98	1.64	1.02	0.94	0.74	1.08
	B	1.32	0.96	1.22	1.24	1.22	0.86	1.04	0.80
	AB	1.60	1.62	1.68	1.98	1.86	1.34	1.54	1.42

1. 2 equal means - unequal cell counts

Table 1-2-1a:
equal means - average $n_i=5$ - n of levels=4*5 - n_i and s_i independent - $\alpha=0.05$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	A	4.76	4.78	4.84	2.78	2.72	4.68	4.76	4.40
	B	4.80	4.96	4.80	2.98	2.86	4.66	4.66	4.22
	AB	5.34	4.72	5.24	4.66	5.28	3.66	4.00	4.24
normal unequal variances (on B)	A	3.68	4.02	3.98	4.94	3.46	4.08	3.70	4.00
	B	5.80	5.04	4.88	3.32	3.22	4.62	4.60	3.90
	AB	6.12	4.90	5.86	6.34	6.10	3.62	4.82	3.90
normal unequal variances (on A and B)	A	6.42	4.84	5.46	3.48	2.94	4.72	5.16	3.98
	B	6.88	5.50	5.92	3.94	3.56	4.98	5.40	3.94
	AB	8.28	5.38	6.62	6.52	7.42	4.10	5.40	3.90
right skewed	A	4.64	4.88	4.84	2.84	2.40	4.56	4.44	4.22
	B	5.46	5.16	5.36	3.00	2.34	4.88	4.94	4.72
	AB	5.14	4.54	5.18	4.96	5.12	3.50	3.92	4.10
exponential continuous	A	5.62	4.94	5.14	4.16	2.56	4.78	4.78	4.42
	B	5.20	5.16	5.20	3.96	2.24	4.66	4.80	4.66
	AB	6.24	4.96	4.66	6.18	5.82	3.42	3.76	4.38
exponential discrete	A	5.94	5.56	5.34	4.50	2.60	5.22	5.16	4.84
	B	4.96	4.88	4.80	3.96	2.18	4.42	4.40	4.66
	AB	6.40	5.08	4.98	6.70	6.30	3.84	3.84	4.42
lognormal (0 / 0.25)	A	4.98	4.96	5.08	3.12	2.74	4.66	4.82	4.08
	B	5.20	4.56	4.70	3.24	2.60	4.48	4.52	4.34
	AB	5.50	4.60	4.80	4.64	5.04	3.50	3.86	4.50
uniform continuous	A	4.74	4.88	4.84	2.64	2.70	4.56	4.44	4.22
	B	5.14	5.16	5.36	2.90	2.58	4.88	4.94	4.72
	AB	4.60	4.54	5.18	4.66	4.74	3.50	3.92	4.10
uniform discrete	A	4.90	4.98	4.96	2.60	2.70	4.56	4.62	4.24
	B	5.70	5.78	5.58	2.96	2.96	5.22	5.32	4.64
	AB	4.88	4.90	4.80	4.72	5.06	3.56	3.50	4.58
left/right skewed	A	4.96	5.02	4.94	2.52	2.34	4.64	4.50	4.30
	B	5.10	4.80	6.36	2.66	2.62	4.54	5.88	4.28
	AB	5.12	4.92	5.34	4.84	5.06	3.66	4.00	4.20
left skewed unequal variances (on B)	A	3.78	3.92	3.68	4.48	3.08	3.62	3.24	3.76
	B	5.62	5.76	5.28	3.10	2.82	5.54	5.04	3.98
	AB	6.30	5.08	6.68	6.40	6.44	3.74	5.12	3.56
left skewed unequal variances (on A and B)	A	6.64	4.98	5.80	3.36	2.66	4.64	5.22	3.66
	B	7.74	5.98	6.64	4.00	3.06	5.38	6.14	4.12
	AB	9.22	5.68	8.42	7.86	9.66	4.50	6.70	4.06

Table 1-2-1b:
equal means - average $n_i=5$ - n of levels=4*5 - n_i and s_i independent - $\alpha=0.01$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	A	1.16	1.00	1.16	0.54	0.50	0.84	0.90	0.98
	B	0.86	0.84	1.02	0.50	0.32	0.58	0.56	0.90
	AB	1.06	0.84	1.04	0.90	0.90	0.50	0.54	1.10
normal unequal variances (on B)	A	0.94	0.82	0.90	1.06	0.52	0.66	0.66	0.74
	B	1.76	0.96	1.22	0.62	0.44	0.86	0.94	0.76
	AB	1.44	1.00	1.12	1.16	1.30	0.44	0.60	0.76
normal unequal variances (on A und B)	A	1.70	1.18	1.26	0.84	0.56	0.98	1.08	0.74
	B	1.86	0.88	1.00	0.88	0.60	0.74	0.78	0.80
	AB	2.72	1.12	1.62	1.58	2.06	0.44	1.00	0.80
right skewed	A	1.06	0.82	0.88	0.50	0.32	0.66	0.74	0.68
	B	1.14	1.18	1.22	0.58	0.40	0.92	0.90	0.98
	AB	1.20	0.90	1.04	1.08	1.18	0.50	0.46	0.98
exponential continuous	A	1.44	1.04	1.08	0.88	0.40	0.88	0.88	1.20
	B	1.36	0.86	1.00	0.86	0.26	0.62	0.80	1.18
	AB	1.78	0.98	0.96	1.40	1.60	0.50	0.52	1.08
exponential discrete	A	1.38	0.84	1.00	0.96	0.34	0.66	0.72	0.96
	B	1.44	0.68	0.84	0.78	0.34	0.54	0.68	1.00
	AB	1.80	0.80	1.02	1.56	1.84	0.42	0.56	0.98
lognormal (0 / 0.25)	A	1.20	1.14	1.10	0.64	0.44	0.96	0.96	1.02
	B	1.04	0.82	0.86	0.62	0.44	0.66	0.68	0.90
	AB	1.32	0.98	1.12	0.96	0.92	0.48	0.42	1.14
uniform continuous	A	0.84	0.82	0.88	0.42	0.38	0.66	0.74	0.68
	B	1.18	1.18	1.22	0.52	0.44	0.92	0.90	0.98
	AB	1.00	0.90	1.04	0.98	0.78	0.50	0.46	0.98
uniform discrete	A	0.80	0.82	0.88	0.40	0.34	0.74	0.76	0.78
	B	1.14	1.08	1.18	0.52	0.46	0.96	1.02	1.12
	AB	0.86	0.86	1.02	1.06	1.02	0.48	0.50	1.00
left/right skewed	A	0.90	0.84	1.02	0.52	0.32	0.54	0.76	0.76
	B	1.18	1.00	1.54	0.46	0.46	0.80	1.18	0.92
	AB	1.06	0.90	1.16	0.94	1.02	0.52	0.70	1.06
left skewed unequal variances (on B)	A	0.66	0.70	0.80	1.02	0.54	0.48	0.42	0.68
	B	1.74	1.48	1.44	0.66	0.64	1.14	1.22	1.14
	AB	1.94	1.32	2.00	1.72	1.96	0.54	1.04	0.94
left skewed unequal variances (on A and B)	A	1.98	1.10	1.64	0.84	0.52	0.82	1.26	0.82
	B	2.28	1.28	1.98	0.80	0.54	1.10	1.40	0.94
	AB	3.26	1.42	2.66	2.10	3.20	0.80	1.72	1.08

Table 1-2-2a:
equal means - average $n_i=5$ - n of levels=4*5 - n_i and s_i dependent - $\alpha=0.05$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal unequal variances small n_i - small s_i	A	1.04	2.10	1.24	3.86	2.64	2.02	1.26	4.34
	B	1.22	2.02	1.32	4.24	2.72	1.86	1.28	4.14
	AB	1.04	1.84	1.28	2.02	1.34	1.30	0.76	3.66
normal unequal variances small n_i - large s_i	A	18.44	10.10	14.34	3.40	3.46	9.56	13.02	4.52
	B	18.64	9.60	14.44	3.74	3.50	8.70	12.68	4.62
	AB	23.60	11.28	17.20	14.04	19.20	8.94	14.24	5.24
left skewed unequal variances small n_i - small s_i	A	1.00	1.15	0.95	3.30	1.72	1.20	0.90	4.45
	B	1.45	2.05	1.00	3.70	2.02	1.70	0.90	4.35
	AB	1.55	2.15	1.25	2.60	1.00	1.35	0.70	3.50
left skewed unequal variances small n_i - large s_i	A	17.2	11.5	19.15	3.05	3.44	10.50	16.30	4.50
	B	19.4	13.4	21.65	4.55	3.88	12.10	19.35	4.70
	AB	24.1	15.3	27.55	17.70	25.64	12.75	23.10	5.20

Table 1-2-2b:
equal means - average $n_i=5$ - n of levels=4*5 - n_i and s_i dependent - $\alpha=0.01$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal unequal variances small n_i - small s_i	A	0.12	0.24	0.14	0.70	0.46	0.18	0.10	0.86
	B	0.08	0.28	0.08	0.82	0.54	0.24	0.06	0.62
	AB	0.22	0.32	0.22	0.34	0.22	0.20	0.14	0.70
normal unequal variances small n_i - large s_i	A	6.92	2.64	4.64	0.72	0.80	2.30	3.72	1.12
	B	7.52	2.70	4.46	0.58	0.56	2.04	3.40	1.38
	AB	9.54	2.90	6.20	4.06	7.06	1.60	3.64	1.66
left skewed unequal variances small n_i - small s_i	A	0.25	0.25	0.25	0.90	0.30	0.20	0.15	0.60
	B	0.25	0.25	0.20	0.65	0.30	0.15	0.10	0.75
	AB	0.35	0.35	0.25	0.60	0.18	0.10	0.15	0.60
left skewed unequal variances small n_i - large s_i	A	6.6	3.35	7.50	0.60	0.66	2.45	5.50	1.10
	B	7.7	4.60	9.30	0.70	0.78	3.30	7.50	1.60
	AB	10.1	5.15	12.35	6.45	10.74	3.25	7.85	1.45

1. 3 unequal means - equal cell counts

Table 1-3-1a:
unequal means - $n_i=10$ - n of levels=2*4 - A sig (0.6*s) - $\alpha=0.05$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	B	4.58	4.76	4.68	4.74	4.56	3.14	3.06	4.30
	AB	4.50	4.72	4.86	5.10	4.84	3.12	3.10	4.48
normal unequal.. variances (B)	B	6.44	6.12	5.58	5.80	5.36	3.88	4.08	5.08
	AB	5.86	5.84	5.62	6.34	5.92	4.18	4.00	5.46
normal unequal variances (A,B)	B	5.94	5.84	5.52	6.12	5.56	3.96	3.80	5.10
	AB	5.62	5.86	5.28	6.52	5.70	3.88	3.66	5.48
right skewed	B	4.72	4.88	4.76	5.06	4.28	3.14	2.76	4.60
	AB	5.08	5.08	5.10	5.56	5.28	3.42	2.94	4.86
exponential continuous	B	4.78	5.30	5.04	8.76	4.14	3.72	3.48	5.10
	AB	4.66	4.84	4.94	9.36	4.98	3.50	3.46	4.52
exponential discrete	B	4.70	4.88	4.94	10.40	3.90	3.52	3.40	4.70
	AB	4.82	5.10	5.14	11.88	5.46	3.52	3.42	4.68
lognormal (0 / 0.25)	B	4.56	5.28	4.86	4.86	4.66	3.48	3.40	5.08
	AB	4.46	5.02	4.72	4.82	4.78	3.28	2.90	4.62
uniform continuous	B	4.90	4.86	4.88	4.96	4.84	3.48	3.22	4.70
	AB	5.18	5.14	5.26	5.34	5.08	3.90	3.58	4.90
uniform discrete	B	4.52	4.72	4.60	4.76	4.34	3.24	3.12	4.58
	AB	4.90	4.84	5.02	5.26	5.14	3.50	3.34	4.62
left/right skewed	B	4.76	4.42	5.02	4.42	5.20	2.88	3.42	4.24
	AB	4.72	4.98	4.78	4.86	4.76	3.44	3.44	4.78
left skewed unequal variances (B)	B	5.40	5.54	4.92	5.24	4.56	3.80	3.52	4.88
	AB	6.26	6.02	6.06	6.70	6.66	4.72	4.16	5.58
left skewed unequal variances (A,B)	B	5.36	4.94	4.90	5.50	5.20	3.18	3.22	4.20
	AB	5.92	5.92	5.56	6.72	6.38	4.54	4.08	5.46

Table 1-3-1b:
unequal means - $n_i=10$ - n of levels=2*4 - A sig (0.6*s) - $\alpha=0.01$

distribution type	effect	param	RT	INT	ART	ART+INT	Puri & Sen	van der Waerden	ATS
normal equal variances	B	0.82	0.84	0.76	0.64	0.74	0.34	0.34	0.74
	AB	0.94	1.10	0.96	1.10	0.92	0.64	0.56	0.96
normal unequal variances (B)	B	1.72	1.32	1.32	1.12	1.30	0.62	0.64	1.02
	AB	1.48	1.32	1.30	1.48	1.60	0.80	0.80	1.28
normal unequal variances (A,B)	B	1.48	1.18	1.26	1.18	1.14	0.68	0.72	0.96
	AB	1.54	1.38	1.32	1.54	1.52	0.86	0.78	1.24
right skewed	B	1.04	0.90	1.02	0.92	0.72	0.42	0.34	0.86
	AB	1.16	1.22	1.16	1.14	1.10	0.54	0.42	1.08
exponential continuous	B	0.92	0.84	0.74	1.94	0.58	0.38	0.38	0.74
	AB	1.00	1.00	0.90	2.32	1.18	0.60	0.48	0.90
exponential discrete	B	0.82	0.98	1.00	2.80	0.72	0.48	0.46	0.84
	AB	0.88	1.16	1.06	3.46	1.38	0.74	0.74	1.00
lognormal (0 / 0.25)	B	1.04	1.26	1.24	1.32	1.24	0.60	0.58	1.18
	AB	0.86	0.90	0.82	0.90	0.90	0.50	0.34	0.82
uniform continuous	B	0.76	0.80	0.84	0.78	0.94	0.52	0.42	0.74
	AB	1.00	1.06	1.26	1.18	0.98	0.54	0.58	0.96
uniform discrete	B	0.94	1.02	1.04	0.94	0.86	0.52	0.40	0.96
	AB	1.18	1.14	1.06	1.28	1.12	0.66	0.54	1.00
left/right skewed	B	0.78	0.82	1.00	0.84	0.96	0.44	0.42	0.72
	AB	1.24	1.16	1.04	1.32	1.18	0.72	0.52	1.12
left skewed unequal variances (B)	B	1.54	1.16	1.18	1.18	1.20	0.70	0.68	0.80
	AB	1.92	1.58	1.80	1.78	1.92	1.10	1.18	1.52
left skewed unequal variances (A,B)	B	1.32	0.90	1.22	1.24	1.22	0.58	0.54	0.76
	AB	1.60	1.60	1.58	1.98	1.86	1.04	1.10	1.36

Table 1-3-2a:
unequal means - $n_i=10$ - n of levels=2*4 - A and B sig (0.8*s) - $\alpha=0.05$

(Only error rates for the test of the interaction are reported.)

distribution type	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal - equal variances	4.50	4.88	4.64	5.10	4.84	1.40	1.36	4.62
normal - uneq. variances (B)	5.86	6.80	5.94	6.34	5.92	2.18	2.00	6.20
normal - uneq. variances (A,B)	5.62	7.56	5.82	6.52	5.70	3.04	2.22	7.06
right skewed	5.08	5.12	5.56	5.56	5.28	1.46	1.34	4.84
exponential - continuous	5.30	6.02	5.64	7.90	6.10	4.48	3.94	5.68
exponential - discrete	5.30	6.06	5.88	8.12	5.76	4.40	4.36	5.70
lognormal (0 / 0.25)	4.46	4.74	4.60	4.82	4.78	1.08	1.14	4.38
uniform - continuous	5.18	4.86	4.62	5.34	5.08	1.80	1.54	4.66
uniform - discrete	5.14	4.74	4.62	5.20	5.12	1.92	1.46	4.50
left/right skewed	4.72	5.02	4.56	4.86	4.76	1.98	1.58	4.82
left skewed - uneq. var. (B)	6.26	6.44	5.66	6.70	6.66	2.94	2.34	5.96
left skewed - uneq. var. (A,B)	5.92	7.26	5.64	6.72	6.38	3.88	2.52	6.76

Table 1-3-2b:
unequal means - $n_i=10$ - n of levels=2*4 - A and B sig (0.8*s) - $\alpha=0.01$

(Only error rates for the test of the interaction are reported.)

distribution type	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal - equal variances	0.94	0.96	0.98	1.10	0.92	0.08	0.08	0.86
normal - uneq. variances (B)	1.48	1.44	1.18	1.48	1.60	0.28	0.30	1.20
normal - uneq. variances (A,B)	1.54	2.06	1.20	1.54	1.52	0.42	0.32	1.54
right skewed	1.16	1.16	1.12	1.14	1.10	0.20	0.16	0.98
exponential - continuous	1.38	1.32	1.42	2.42	1.72	0.68	0.66	1.26
exponential - discrete	1.32	1.30	1.34	2.60	1.76	0.70	0.58	1.12
lognormal (0 / 0.25)	0.86	0.80	0.88	0.90	0.90	0.16	0.10	0.66
uniform - continuous	1.00	0.98	0.88	1.18	0.98	0.12	0.18	0.80
uniform - discrete	1.18	1.12	0.98	1.34	1.32	0.10	0.12	0.90
left/right skewed	1.24	1.20	1.02	1.32	1.18	0.24	0.14	1.18
left skewed - uneq. var. (B)	1.92	1.88	1.54	1.78	1.92	0.44	0.50	1.62
left skewed - uneq. var. (A,B)	1.60	1.86	1.42	1.98	1.86	0.76	0.54	1.66

Table 1-3-3:**unequal means - $n_i=10$ - n of levels=2*4 - $\alpha=0.05$** **influence of significant effects on the type I error rates for the interaction AB**

(This is a summary with excerpts from tables 1-1-1a, 1-3-1a and 1-3-2a.)

distribution type	signif effects	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal	-	5.54	5.50	5.48	5.30	5.56	5.46	5.54	5.48
equal variances	A	4.50	4.72	4.86	5.10	4.84	3.12	3.10	4.48
	A, B	4.50	4.88	4.64	5.10	4.84	1.40	1.36	4.62
normal	-	5.68	5.34	5.58	6.98	6.24	5.20	5.44	5.28
unequal variances	A	5.86	5.84	5.62	6.34	5.92	4.18	4.00	5.46
(on B)	A, B	5.86	6.80	5.94	6.34	5.92	2.18	2.00	6.20
normal	-	5.76	5.30	5.52	6.80	6.12	5.12	5.38	5.26
unequal variances	A	5.62	5.86	5.28	6.52	5.70	3.88	3.66	5.48
(on A and B)	A, B	5.62	7.56	5.82	6.52	5.70	3.04	2.22	7.06
right skewed	-	5.00	5.40	5.22	5.42	4.82	5.18	5.20	5.36
	A	5.08	5.08	5.10	5.56	5.28	3.42	2.94	4.86
	A, B	5.08	5.12	5.56	5.56	5.28	1.46	1.34	4.84
exponential	-	4.68	5.66	5.32	6.12	5.42	5.22	4.92	5.32
continuous	A	4.66	4.84	4.94	9.36	4.98	3.50	3.46	4.52
	A, B	5.30	6.02	5.64	7.90	6.10	4.48	3.94	5.68
exponential	-	4.54	5.54	5.28	6.58	5.54	5.08	4.86	5.38
discrete	A	4.82	5.10	5.14	11.88	5.46	3.52	3.42	4.68
	A, B	6.06	5.88	8.12	5.76	4.40	4.36	5.70	6.06
lognormal (0 / 0.25)	-	4.46	4.88	4.86	4.82	4.78	4.62	4.44	4.54
	A	4.46	5.02	4.72	4.82	4.78	3.28	2.90	4.62
	A, B	4.46	4.74	4.60	4.82	4.78	1.08	1.14	4.38
uniform	-	5.18	5.28	5.02	5.34	5.08	5.06	4.74	5.06
continuous	A	5.18	5.14	5.26	5.34	5.08	3.90	3.58	4.90
	A, B	5.18	4.86	4.62	5.34	5.08	1.80	1.54	4.66
uniform	-	5.12	5.06	5.08	5.94	5.80	4.98	5.02	5.02
discrete	A	4.90	4.84	5.02	5.26	5.14	3.50	3.34	4.62
	A, B	5.14	4.74	4.62	5.20	5.12	1.92	1.46	4.50
left/right skewed	-	5.12	4.18	7.02	4.34	4.44	4.12	6.66	4.16
	A	4.72	4.98	4.78	4.86	4.76	3.44	3.44	4.78
	A, B	4.72	5.02	4.56	4.86	4.76	1.98	1.58	4.82
left skewed	-	5.12	5.08	5.04	7.12	5.52	4.88	5.02	4.98
unequal variances	A	6.26	6.02	6.06	6.70	6.66	4.72	4.16	5.58
(on B)	A, B	6.26	6.44	5.66	6.70	6.66	2.94	2.34	5.96
left skewed	-	5.16	5.20	4.96	7.24	5.74	4.90	4.70	5.08
unequal variances	A	5.92	5.92	5.56	6.72	6.38	4.54	4.08	5.46
(on A and B)	A, B	5.92	7.26	5.64	6.72	6.38	3.88	2.52	6.76

Table 1-3-4:
unequal means - $n_i=10$ - n of levels=2*4 - $\alpha=0.05$
influence of significant effects on the type I error rates for effect B

(This is a summary with excerpts from tables 1-1-1a nad 1-3-1a),

distribution type	signif effects	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal	-	4.58	4.62	4.72	4.74	4.56	4.32	4.46	4.34
equal variances	A	5.14	5.16	5.34	5.16	4.56	3.52	3.52	5.04
normal	-	6.44	6.00	5.52	5.80	5.36	5.56	5.20	5.20
unequal variances (B)	A	5.66	5.76	5.08	5.76	5.36	3.78	3.34	5.42
normal	-	5.94	5.80	5.40	6.12	5.56	5.46	5.08	5.24
unequal variances (A,B)	A	5.80	6.38	5.36	6.20	5.56	4.64	3.86	5.94
right skewed	-	4.72	4.92	4.94	5.06	4.28	4.66	4.62	4.82
	A	5.08	5.28	5.02	5.56	5.28	5.06	4.74	5.06
exponential	-	4.76	5.44	5.32	5.52	4.14	4.98	4.66	5.18
continuous	A	4.78	5.30	5.04	8.76	4.14	3.72	3.48	5.10
exponential	-	4.60	5.20	5.26	5.92	3.92	4.90	4.94	5.08
discrete	A	4.70	4.88	4.94	10.40	3.90	3.52	3.40	4.70
lognormal (0 / 0.25)	-	4.56	4.90	4.92	4.86	4.66	4.68	4.66	4.86
	A	4.56	5.28	4.86	4.86	4.66	3.48	3.40	5.08
uniform	-	4.90	4.92	4.94	4.96	4.84	4.66	4.62	4.82
continuous	A	4.90	4.86	4.88	4.96	4.84	3.48	3.22	4.70
uniform	-	4.90	4.82	4.70	4.80	4.30	4.48	4.48	4.62
discrete	A	4.86	4.82	4.88	4.82	4.34	3.98	3.72	4.80
left/right skewed	-	5.16	5.12	5.20	4.42	5.20	4.90	4.96	5.00
	A	4.92	4.36	5.28	4.36	5.20	3.10	3.50	4.30
left skewed	-	5.40	5.38	4.58	5.24	4.56	5.14	4.32	4.84
unequal variances (B)	A	5.22	5.84	4.72	5.84	5.56	3.82	3.30	5.38
left skewed	-	5.36	5.24	5.06	5.50	5.20	4.92	4.78	4.72
unequal variances (A,B)	A	5.86	11.10	5.76	7.52	5.20	9.08	4.46	10.96

1. 4 unequal means - unequal cell counts

Table 1-4-1a:
unequal means - average $n_i=5$ - n of levels=4*5 - A sig (0.6*s) - a=0.05

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	B	4.80	5.10	5.14	4.14	3.68	3.44	3.28	4.14
	AB	5.34	4.74	5.12	4.80	5.32	2.22	2.66	4.22
normal unequal variances (B)	B	5.80	5.12	4.94	4.52	3.88	3.70	3.62	4.02
	AB	6.12	5.40	5.76	6.42	6.32	2.56	2.82	3.86
normal unequal variances (A,B)	B	6.88	5.66	5.92	5.32	4.62	3.96	4.20	3.90
	AB	8.28	5.92	7.04	6.60	7.56	3.04	3.98	3.96
right skewed	B	5.46	5.60	5.60	4.74	4.10	3.74	3.62	4.56
	AB	5.14	5.32	5.72	5.10	5.38	2.20	2.48	4.86
exponential continuous	B	3.58	3.92	3.98	7.66	3.64	2.74	2.84	4.02
	AB	4.92	4.34	4.24	5.92	4.50	1.88	1.90	4.02
exponential discrete	B	3.30	3.42	3.16	9.54	3.78	2.42	2.30	3.94
	AB	5.16	4.28	4.10	7.30	5.08	1.90	1.90	4.04
lognormal (0 / 0.25)	B	5.20	4.94	5.40	4.04	3.44	3.36	3.48	4.38
	AB	5.50	4.86	5.50	4.82	5.24	2.06	2.66	4.62
uniform continuous	B	5.14	5.12	5.26	3.68	3.90	4.00	3.58	4.64
	AB	4.60	4.54	4.90	4.44	4.66	2.10	1.92	4.08
uniform discrete	B	5.54	5.48	5.40	4.12	4.08	4.02	3.62	4.78
	AB	4.98	4.74	4.70	5.00	5.18	2.10	1.76	4.46
left/right skewed	B	5.10	4.60	6.02	3.92	3.88	3.42	4.20	4.28
	AB	5.12	4.70	5.28	5.00	5.04	2.12	2.22	4.12
left skewed unequal variances (B)	B	5.62	5.74	5.52	3.34	3.04	4.32	4.42	4.14
	AB	6.30	5.18	6.54	6.28	6.40	2.78	3.34	3.94
left skewed unequal variances (A,B)	B	7.74	5.64	6.54	4.62	3.78	4.04	4.64	4.22
	AB	9.22	5.96	7.86	7.68	9.50	3.36	4.42	3.86

Table 1-4-1b:
unequal means - average $n_i=5$ - n of levels=4*5 - A sig (0.6*s) - $\alpha=0.01$

distribution type	effect	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	B	0.86	0.96	0.94	0.80	0.80	0.42	0.38	0.98
	AB	1.06	0.98	0.96	0.88	1.04	0.32	0.34	1.10
normal unequal variances (B)	B	1.76	1.14	1.16	1.16	1.04	0.60	0.56	0.80
	AB	1.44	1.10	1.14	1.18	1.34	0.32	0.38	0.88
normal unequal variances (A,B)	B	1.86	1.04	1.28	1.22	0.94	0.56	0.58	0.78
	AB	2.72	1.28	1.68	1.52	2.08	0.48	0.56	0.88
right skewed	B	1.14	1.36	1.32	0.90	0.68	0.58	0.68	1.22
	AB	1.20	1.24	1.20	1.26	1.34	0.28	0.24	1.26
exponential continuous	B	0.94	0.72	0.78	1.70	0.68	0.48	0.54	0.88
	AB	1.50	0.88	0.84	1.40	1.34	0.14	0.16	1.02
exponential discrete	B	0.98	0.60	0.64	2.14	0.62	0.38	0.38	0.88
	AB	1.46	0.62	0.76	1.96	1.32	0.12	0.16	0.90
lognormal (0 / 0.25)	B	1.04	1.06	1.18	0.68	0.52	0.40	0.58	0.92
	AB	1.32	1.06	1.24	0.94	1.00	0.26	0.14	1.00
uniform continuous	B	1.18	1.18	1.34	0.72	0.70	0.64	0.56	1.14
	AB	1.00	0.90	0.96	0.88	0.84	0.34	0.26	0.96
uniform discrete	B	1.18	1.20	1.12	0.82	0.80	0.68	0.58	1.26
	AB	0.86	0.84	0.80	0.94	0.80	0.22	0.16	0.94
left/right skewed	B	1.18	1.00	1.42	0.74	0.66	0.58	0.72	0.80
	AB	1.06	0.94	1.10	1.00	1.00	0.38	0.32	1.12
left skewed unequal variances (B)	B	1.74	1.46	1.62	0.66	0.70	0.88	1.02	1.14
	AB	1.94	1.40	1.98	1.76	1.98	0.58	0.72	0.88
left skewed unequal variances (A,B)	B	2.28	1.22	1.90	0.88	0.74	0.66	0.86	0.84
	AB	3.26	1.52	2.64	2.12	3.24	0.64	1.08	1.12

Table 1-4-2a:**unequal means - average $n_i=5$ - n of levels=4*5 - A and B sig (0.8*s) - $\alpha=0.05$**

(Only error rates for the test of the interaction are reported.)

distribution type	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal - equal variances	5.34	4.60	5.28	4.82	5.34	0.86	0.76	4.28
normal - uneq. variances (B)	6.12	5.54	5.74	6.24	6.28	0.88	1.12	3.98
normal - uneq. variances (A,B)	8.28	6.68	6.94	6.76	7.24	1.86	1.92	4.34
right skewed	5.14	5.60	6.84	5.14	5.72	0.90	0.72	5.54
exponential - continuous	4.42	4.52	4.22	5.48	4.34	2.04	2.22	4.40
exponential - discrete	4.52	4.28	3.94	5.40	4.48	2.04	1.80	4.64
lognormal (0 / 0.25)	5.50	5.22	5.96	4.94	5.28	0.52	0.54	4.46
uniform - continuous	4.60	3.60	5.00	4.44	4.78	0.72	0.74	4.52
uniform - discrete	4.44	3.74	4.68	4.68	4.34	0.68	0.70	4.64
left/right skewed	5.12	3.54	4.98	4.82	5.16	0.78	0.74	4.16
left skewed - uneq. var. (B)	6.30	5.30	5.94	6.22	6.32	1.34	1.46	4.00
left skewed - uneq. var. (A,B)	9.22	6.24	6.96	7.46	9.20	2.30	2.10	3.92

Table 1-4-2b:**unequal means - average $n_i=5$ - n of levels=4*5 - A and B sig (0.8*s) - $\alpha=0.01$**

(Only error rates for the test of the interaction are reported.)

distribution type	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal - equal variances	1.06	0.94	0.94	0.86	1.00	0.14	0.14	1.02
normal - uneq. variances (B)	1.44	1.06	1.32	1.12	1.30	0.14	0.14	0.90
normal - uneq. variances (A,B)	2.72	1.62	1.80	1.54	2.18	0.42	0.32	0.90
right skewed	1.20	1.28	1.54	1.20	1.44	0.10	0.16	1.62
exponential - continuous	1.46	0.90	0.90	1.22	1.02	0.16	0.12	1.00
exponential - discrete	1.42	0.76	0.80	1.36	1.10	0.12	0.08	0.94
lognormal (0 / 0.25)	1.32	1.04	1.20	1.06	1.04	0.04	0.04	1.26
uniform - continuous	1.00	0.78	0.92	0.94	0.86	0.06	0.02	1.04
uniform - discrete	0.90	0.74	1.00	1.04	1.10	0.08	0.08	1.00
left/right skewed	1.06	0.66	0.92	0.84	0.92	0.12	0.12	1.02
left skewed - uneq. var. (B)	1.94	1.26	1.80	1.72	2.08	0.20	0.22	1.02
left skewed - uneq. var. (A,B)	3.26	1.86	2.18	2.12	3.12	0.46	0.46	1.00

Table 1-4-3:
unequal means - average $n_i=5$ - n of levels=4*5 - $\alpha=0.05$
influence of sig effects on the type I error rates for the interaction AB

(This is a summary with excerpts from tables 1-2-1a, 1-4-1a and 1-4-2a.)

distribution type	signif effects	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal equal variances	-	4.76	4.78	4.84	2.78	2.72	4.68	4.76	4.40
	A	5.34	4.74	5.12	4.80	5.32	2.22	2.66	4.22
	A, B	5.34	4.60	5.28	4.82	5.34	0.86	0.76	4.28
normal unequal variances (on B)	-	3.68	4.02	3.98	4.94	3.46	4.08	3.70	4.00
	A	6.12	5.40	5.76	6.42	6.32	2.56	2.82	3.86
	A, B	6.12	5.54	5.74	6.24	6.28	0.88	1.12	3.98
normal unequal variances (on A and B)	-	6.42	4.84	5.46	3.48	2.94	4.72	5.16	3.98
	A	8.28	5.92	7.04	6.60	7.56	3.04	3.98	3.96
	A, B	8.28	6.68	6.94	6.76	7.24	1.86	1.92	4.34
right skewed	-	4.64	4.88	4.84	2.84	2.40	4.56	4.44	4.22
	A	5.14	5.32	5.72	5.10	5.38	2.20	2.48	4.86
	A, B	5.14	5.60	6.84	5.14	5.72	0.90	0.72	5.54
exponential continuous	-	6.24	4.96	4.66	6.18	5.82	3.42	3.76	4.38
	A	4.92	4.34	4.24	5.92	4.50	1.88	1.90	4.02
	A, B	4.42	4.52	4.22	5.48	4.34	2.04	2.22	4.40
exponential discrete	-	6.40	5.08	4.98	6.70	6.30	3.84	3.84	4.42
	A	5.16	4.28	4.10	7.30	5.08	1.90	1.90	4.04
	A, B	4.52	4.28	3.94	5.40	4.48	2.04	1.80	4.64
lognormal (0 / 0.25)	-	5.50	4.60	4.80	4.64	5.04	3.50	3.86	4.50
	A	5.50	4.86	5.50	4.82	5.24	2.06	2.66	4.62
	A, B	5.50	5.22	5.96	4.94	5.28	0.52	0.54	4.46
uniform continuous	-	4.60	4.54	5.18	4.66	4.74	3.50	3.92	4.10
	A	4.60	4.54	4.90	4.44	4.66	2.10	1.92	4.08
	A, B	4.60	3.60	5.00	4.44	4.78	0.72	0.74	4.52
uniform discrete	-	4.90	4.98	4.96	2.60	2.70	4.56	4.62	4.24
	A	4.98	4.74	4.70	5.00	5.18	2.10	1.76	4.46
	A, B	4.44	3.74	4.68	4.68	4.34	0.68	0.70	4.64
left/right skewed	-	4.96	5.02	4.94	2.52	2.34	4.64	4.50	4.30
	A	5.12	4.70	5.28	5.00	5.04	2.12	2.22	4.12
	A, B	5.12	3.54	4.98	4.82	5.16	0.78	0.74	4.16
left skewed unequal variances (on B)	-	3.78	3.92	3.68	4.48	3.08	3.62	3.24	3.76
	A	6.30	5.18	6.54	6.28	6.40	2.78	3.34	3.94
	A, B	6.30	5.30	5.94	6.22	6.32	1.34	1.46	4.00
left skewed unequal variances (on A and B)	-	6.64	4.98	5.80	3.36	2.66	4.64	5.22	3.66
	A	9.22	5.96	7.86	7.68	9.50	3.36	4.42	3.86
	A, B	9.22	6.24	6.96	7.46	9.20	2.30	2.10	3.92

Table 1-4-5:
unequal means - average $n_i=5$ - n of levels=4*5 - $\alpha=0.05$
influence of sig effects on the type I error rates for effect B

(This is a summary with excerpts from table 1-2-1a and 1-4-1a.)

distribution type	signif effects	param	RT	INT	ART	ART+ INT	Puri & Sen	van der Waerden	ATS
normal	-	4.80	4.96	4.80	2.98	2.86	4.66	4.66	4.22
equal variances	A	4.80	5.10	5.14	4.14	3.68	3.44	3.28	4.14
normal	-	5.80	5.04	4.88	3.32	3.22	4.62	4.60	3.90
unequal variances (B)	A	5.80	5.12	4.94	4.52	3.88	3.70	3.62	4.02
normal	-	6.88	5.50	5.92	3.94	3.56	4.98	5.40	3.94
unequal variances (A,B)	A	6.88	5.66	5.92	5.32	4.62	3.96	4.20	3.90
right skewed	-	5.46	5.16	5.36	3.00	2.34	4.88	4.94	4.72
	A	5.46	5.60	5.60	4.74	4.10	3.74	3.62	4.56
exponential	-	5.20	5.16	5.20	3.96	2.24	4.66	4.80	4.66
continuous	A	3.58	3.92	3.98	7.66	3.64	2.74	2.84	4.02
exponential	-	5.10	4.36	4.42	3.74	1.76	4.24	3.96	4.34
discrete	A	3.30	3.42	3.16	9.54	3.78	2.42	2.30	3.94
lognormal (0 / 0.25)	-	5.20	4.56	4.70	3.24	2.60	4.48	4.52	4.34
	A	5.20	4.94	5.40	4.04	3.44	3.36	3.48	4.38
uniform	-	5.14	5.16	5.36	2.90	2.58	4.88	4.94	4.72
continuous	A	5.14	5.12	5.26	3.68	3.90	4.00	3.58	4.64
uniform	-	5.70	5.78	5.58	2.96	2.96	5.22	5.32	4.64
discrete	A	5.54	5.48	5.40	4.12	4.08	4.02	3.62	4.78
left/right skewed	-	5.10	4.80	6.36	2.66	2.62	4.54	5.88	4.28
	A	5.10	4.60	6.02	3.92	3.88	3.42	4.20	4.28
left skewed	-	5.62	5.76	5.28	3.10	2.82	5.54	5.04	3.98
unequal variances (B)	A	5.62	5.74	5.52	3.34	3.04	4.32	4.42	4.14
left skewed	-	7.74	5.98	6.64	4.00	3.06	5.38	6.14	4.12
unequal variances (A,B)	A	7.74	5.64	6.54	4.62	3.78	4.04	4.64	4.22

1.5 Figures

type I error rates of interaction effects

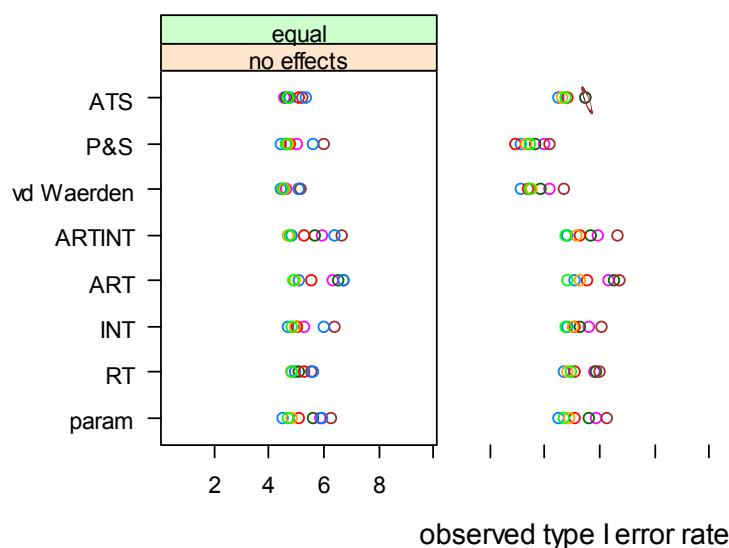


Figure A-1: type I error rates of interaction effects for equal and unequal cell counts and the situations of no other effects, one sig main effect and two sig main effects

1.6 ART median and WA

Table 1-6-1a:
equal means - equal cell counts $n_i=10$ - n of levels=2*4 - $\alpha=0.05$

distribution type	ART median			Wilcoxon Analysis		
	A	B	AB	A	B	AB
normal - equal variances	12.56	15.68	12.82	6.02	5.40	6.02
normal - uneq. variances (B)	11.60	17.08	13.04	7.48	8.86	8.62
normal - uneq. variances (A,B)	11.52	16.40	13.50	7.48	8.78	8.40
right skewed	19.02	29.04	23.28	6.40	6.00	6.72
uniform	26.40	47.32	34.96	17.16	21.40	21.42
left/right skewed	20.68	33.14	27.48	5.14	5.24	5.98
left skewed - uneq. var. (B)	19.94	32.24	26.50	8.92	9.56	10.10
left skewed - uneq. var. (A,B)	19.74	32.46	26.88	8.68	9.66	9.86

Table 1-6-2b:
equal means - equal cell counts $n_i=10$ - n of levels=2*4 - $\alpha=0.01$

distribution type	ART median			Wilcoxon Analysis		
	A	B	AB	A	B	AB
normal - equal variances	4.12	4.66	4.10	1.46	1.00	1.34
normal - uneq. variances (B)	3.44	5.68	4.22	2.14	2.36	2.52
normal - uneq. variances (A,B)	3.38	5.48	4.14	1.90	2.34	2.44
right skewed	8.40	12.36	9.66	1.32	1.42	1.64
uniform	25.16	27.44	17.44	7.06	10.36	10.02
left/right skewed	9.86	15.72	12.50	1.32	1.04	1.46
left skewed - uneq. var. (B)	8.08	15.52	11.86	2.48	2.88	3.30
left skewed - uneq. var. (A,B)	8.36	14.80	11.82	2.50	2.78	3.36

Table 1-6-2a:
equal means - unequal cell counts average $n_i=5$ - n of levels=4*5 - $\alpha=0.05$

distribution type	ART median			Wilcoxon Analysis		
	A	B	AB	A	B	AB
normal - equal variances	11.12	11.30	12.30	7.96	7.64	9.12
normal - uneq. variances (B)	9.28	11.80	11.92	10.48	10.44	12.68
normal - uneq. variances (A,B)	9.18	10.12	13.18	12.22	12.04	14.36
right skewed	18.68	22.18	24.10	9.62	10.82	11.44
uniform	41.32	45.48	44.36	37.94	43.30	62.14
left/right skewed	27.54	30.52	31.92	7.76	7.50	8.56
left skewed - uneq. var. (B)	22.44	28.92	27.96	10.32	11.82	15.58
left skewed - uneq. var. (A,B)	23.88	28.82	31.04	12.26	14.14	16.36

Table 1-6-2b:
equal means - unequal cell counts average $n_i=5$ - n of levels=4*5 - $\alpha=0.01$

distribution type	ART median			Wilcoxon Analysis		
	A	B	AB	A	B	AB
normal - equal variances	2.92	2.82	2.94	2.00	1.84	2.10
normal - uneq. variances (B)	2.48	3.30	3.16	2.88	3.26	4.28
normal - uneq. variances (A,B)	2.46	2.28	3.52	3.84	3.54	4.62
right skewed	7.28	8.70	8.52	2.86	3.66	3.36
uniform	20.96	29.20	20.96	20.88	25.96	46.12
left/right skewed	11.68	12.94	12.24	1.96	2.06	2.22
left skewed - uneq. var. (B)	8.56	13.42	11.44	3.12	4.14	5.54
left skewed - uneq. var. (A,B)	9.46	12.52	12.94	3.70	4.88	5.90

1. 7 Gao and Alvo interaction test

Table 1-7-1:
equal means - equal cell counts $n_i=10$ - n of levels=2*4

distribution type	$\alpha=0.05$		$\alpha=0.01$	
	null model	main effect A significant	null model	main effect A significant
normal - equal variances	9.22	9.34	3.36	3.44
normal - uneq. variances (B)	9.20	10.54	3.50	4.04
normal - uneq. variances (A,B)	9.06	10.88	3.24	3.88
right skewed	9.10	9.74	3.70	3.90
uniform	8.98	8.86	3.26	3.28
left/right skewed	9.20	9.04	3.80	3.54
left skewed - uneq. var. (B)	9.48	10.06	3.42	3.92
left skewed - uneq. var. (A,B)	8.74	9.54	3.26	3.56